

# Biophysical models of synaptic plasticity

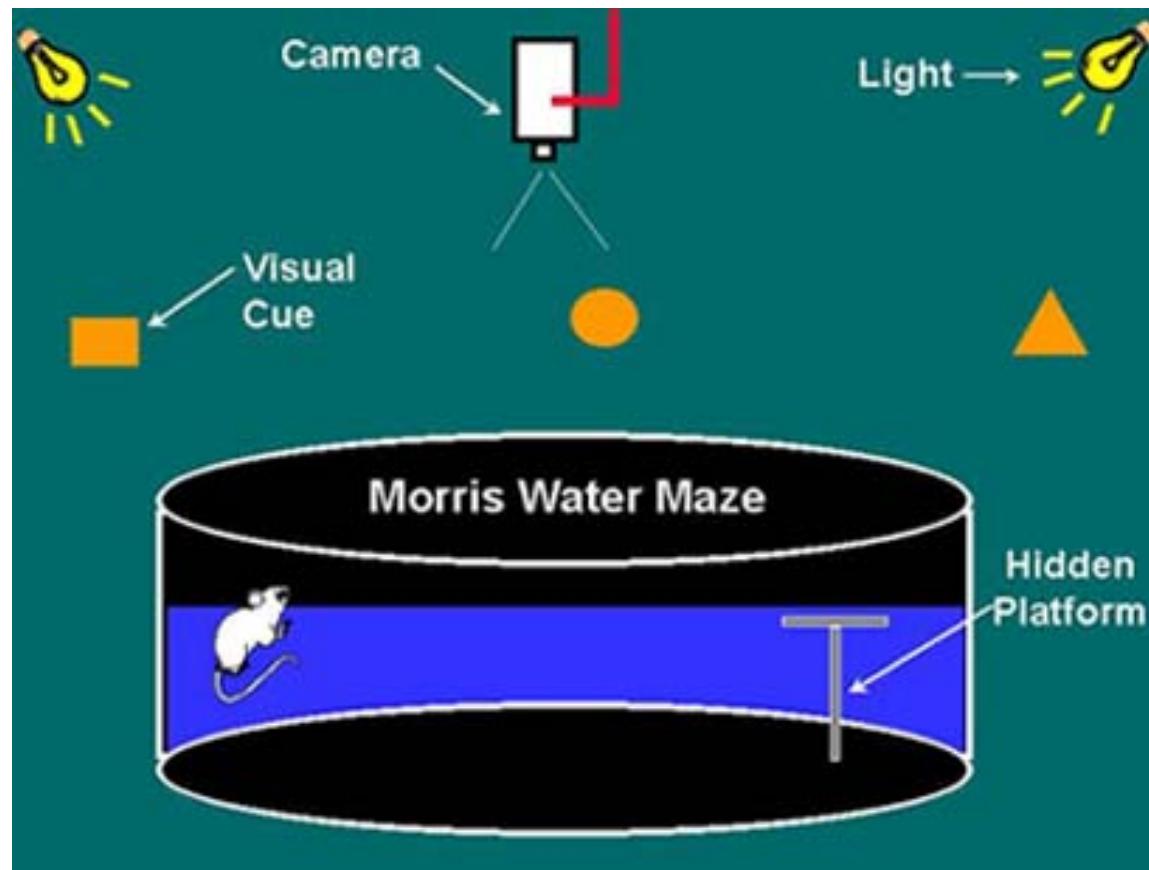
Oct 30<sup>th</sup>, 2015

Michael Graupner

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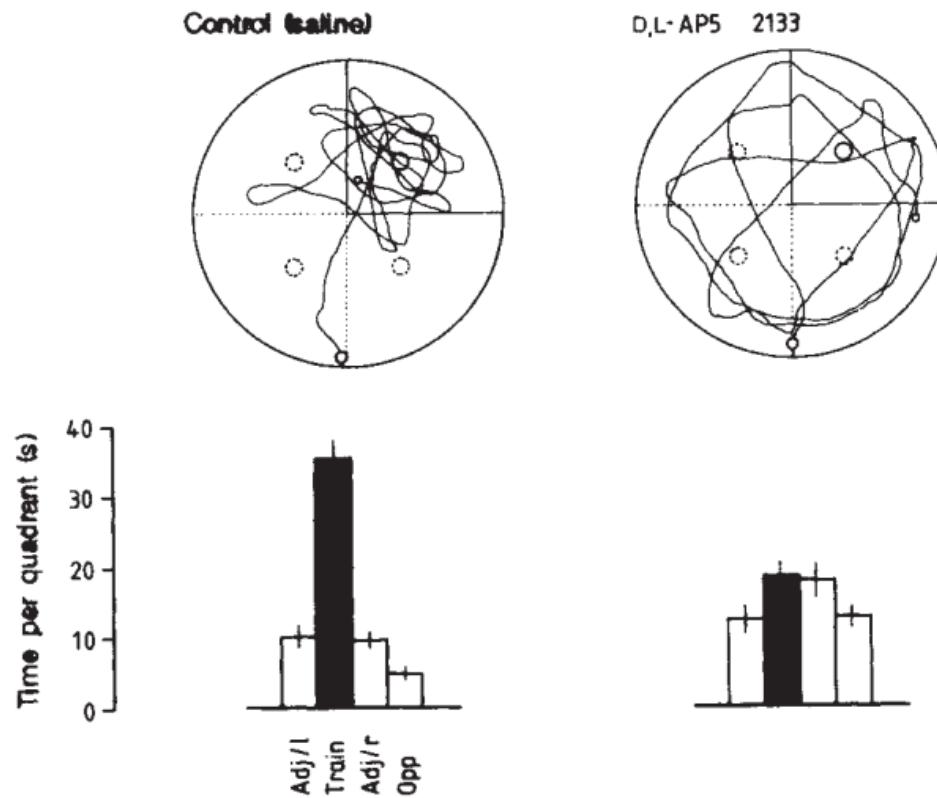
<http://www.biomedicale.univ-paris5.fr/~mgraupe/>

# Why are we interested in synaptic plasticity ?



[Morris *et al.*, 1986]

# Relation between LTP and learning/memory



- NMDA receptor required to learn platform location [Morris *et al.*, 1986]
- NMDA receptor required to form spatial memories (place fields)

[McHugh *et al.* 1996]

# Outline

## 1. Synaptic plasticity : introduction

1.1 Synaptic transmission

1.2 Synaptic plasticity : induction / maintenance / states

## 2. Biological machinery of synaptic plasticity

2.1 NMDA receptor activation required

2.2 Postsynaptic calcium required

## 3. Biophysical models of synaptic plasticity

3.1 Calcium-control hypothesis

3.2 Models of processes reading out the calcium signal

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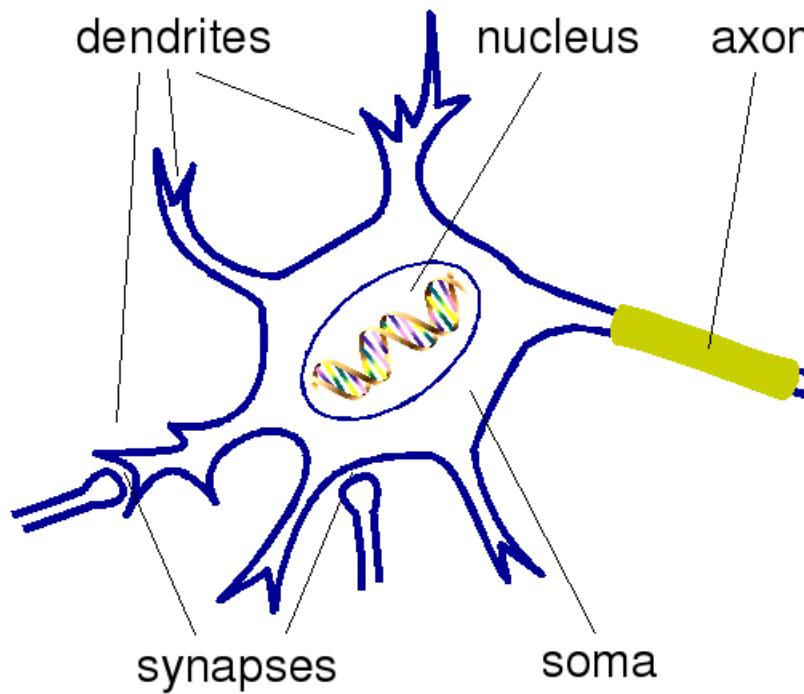
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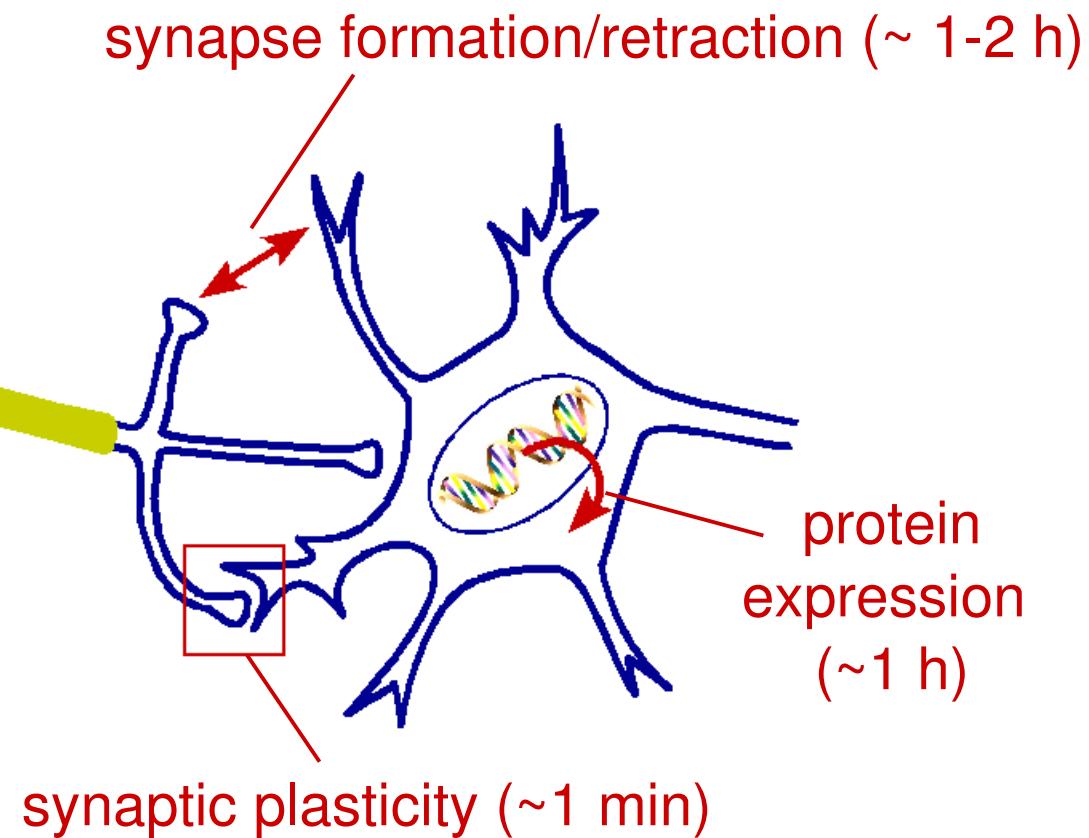
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# Different forms of plasticity

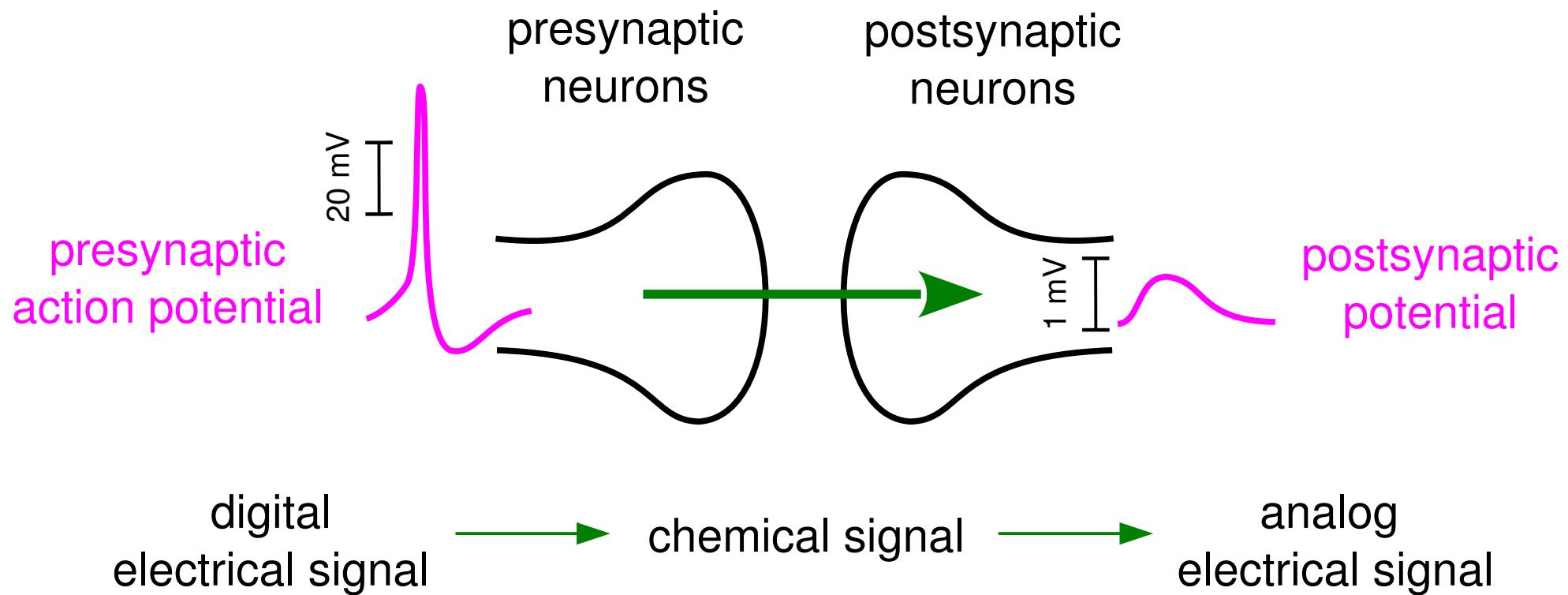
## structure of neurons



## changes related to neural activity

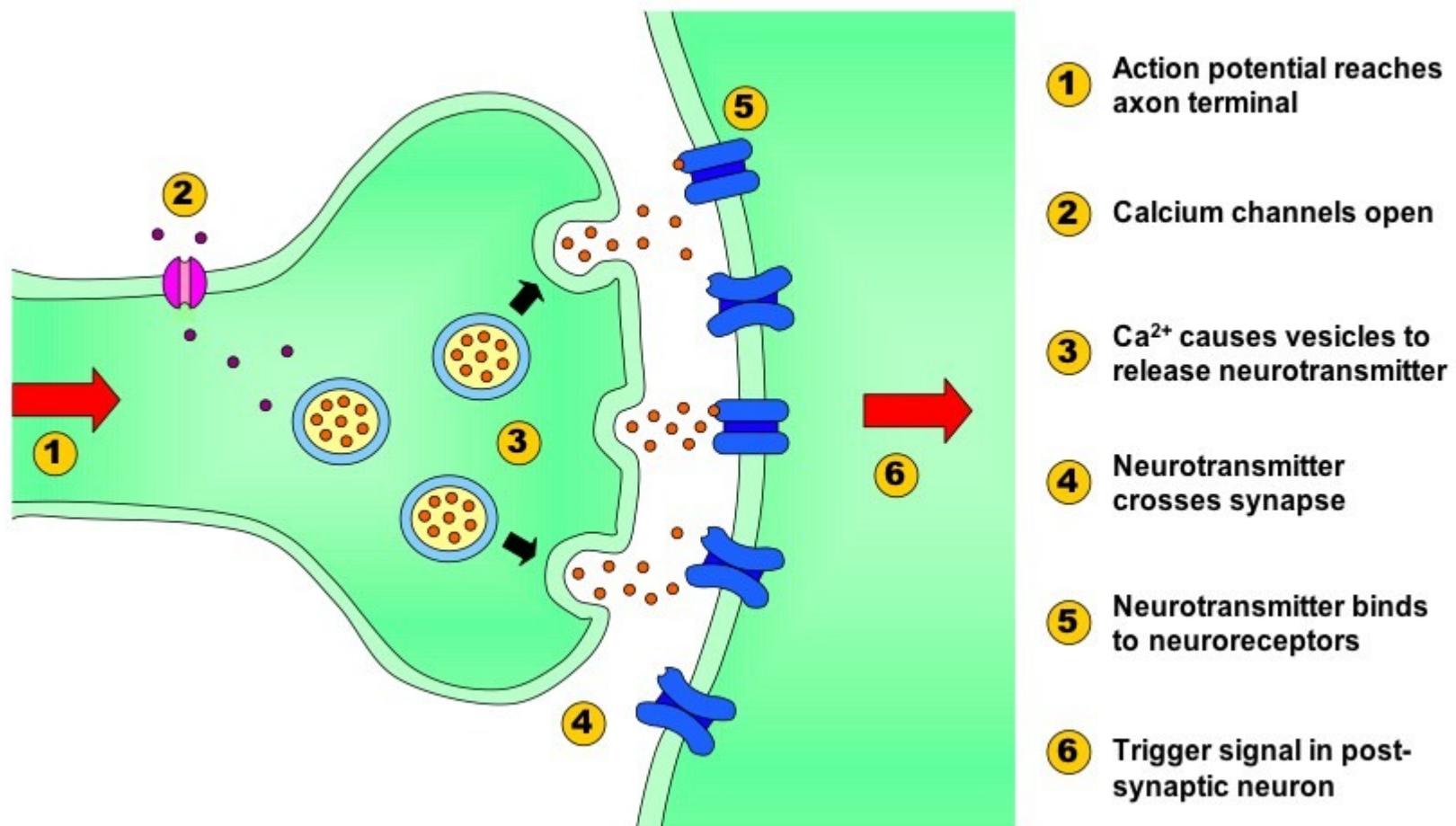


# Chemical synapse : transmits electrical signals



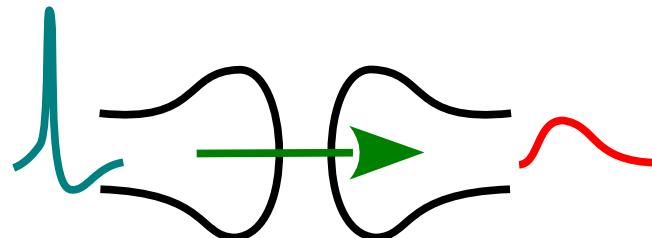
- directional transmission
- conversion of signals allows for flexibility/plasticity

# Chemical synapse : underlying biological machinery



# Chemical synapse : excitatory or inhibitory

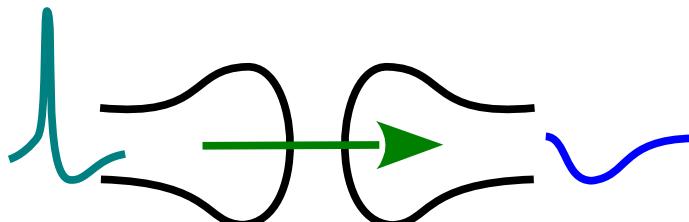
## Excitatory synapse



depolarization:  
*excitatory postsynaptic  
potential (EPSP)*

neurotransmitter	receptor
glutamate	AMPA, NMDA
acetylcholine	nAChR, mAChR
catecholamines	G-protein-coupled receptors
serotonin	5-HT <sub>3</sub> , ...
histamine	G-protein-coupled receptors

## Inhibitory synapse

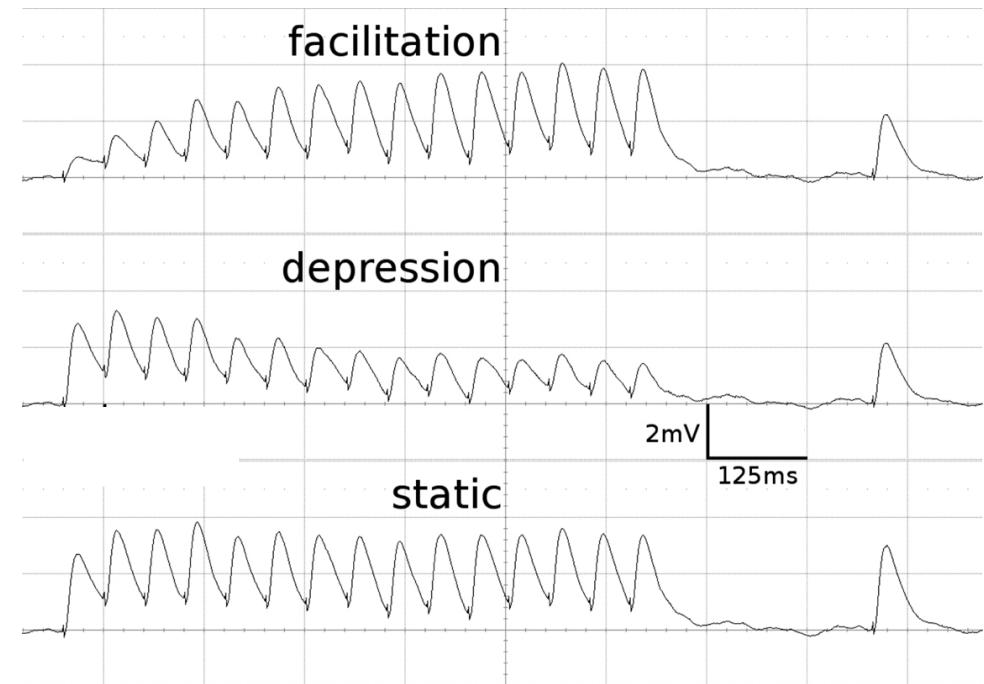
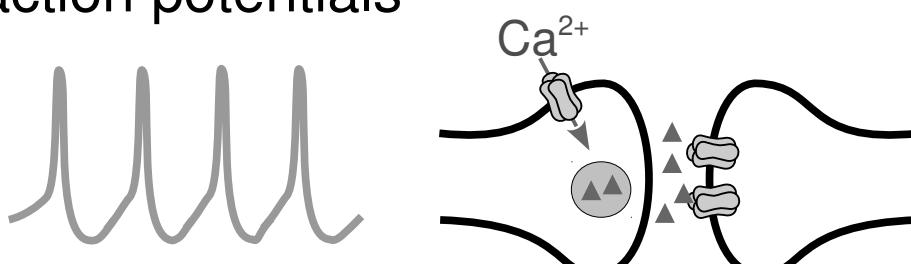


hyperpolarization:  
*Inhibitory postsynaptic  
potential (IPSP)*

neurotransmitter	receptor
GABA	GABA <sub>A</sub> , GABA <sub>B</sub>
glycine	GlyR

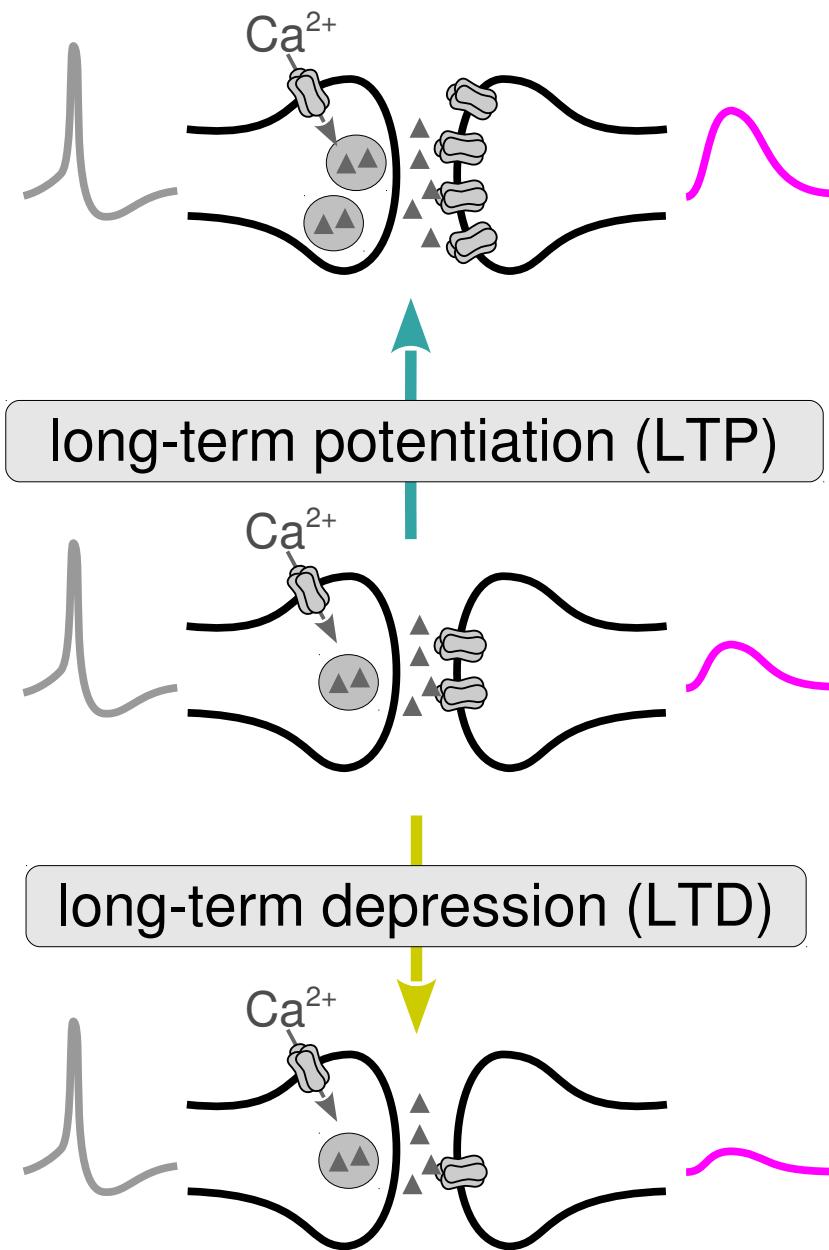
# Short-term synaptic plasticity

train of presynaptic action potentials



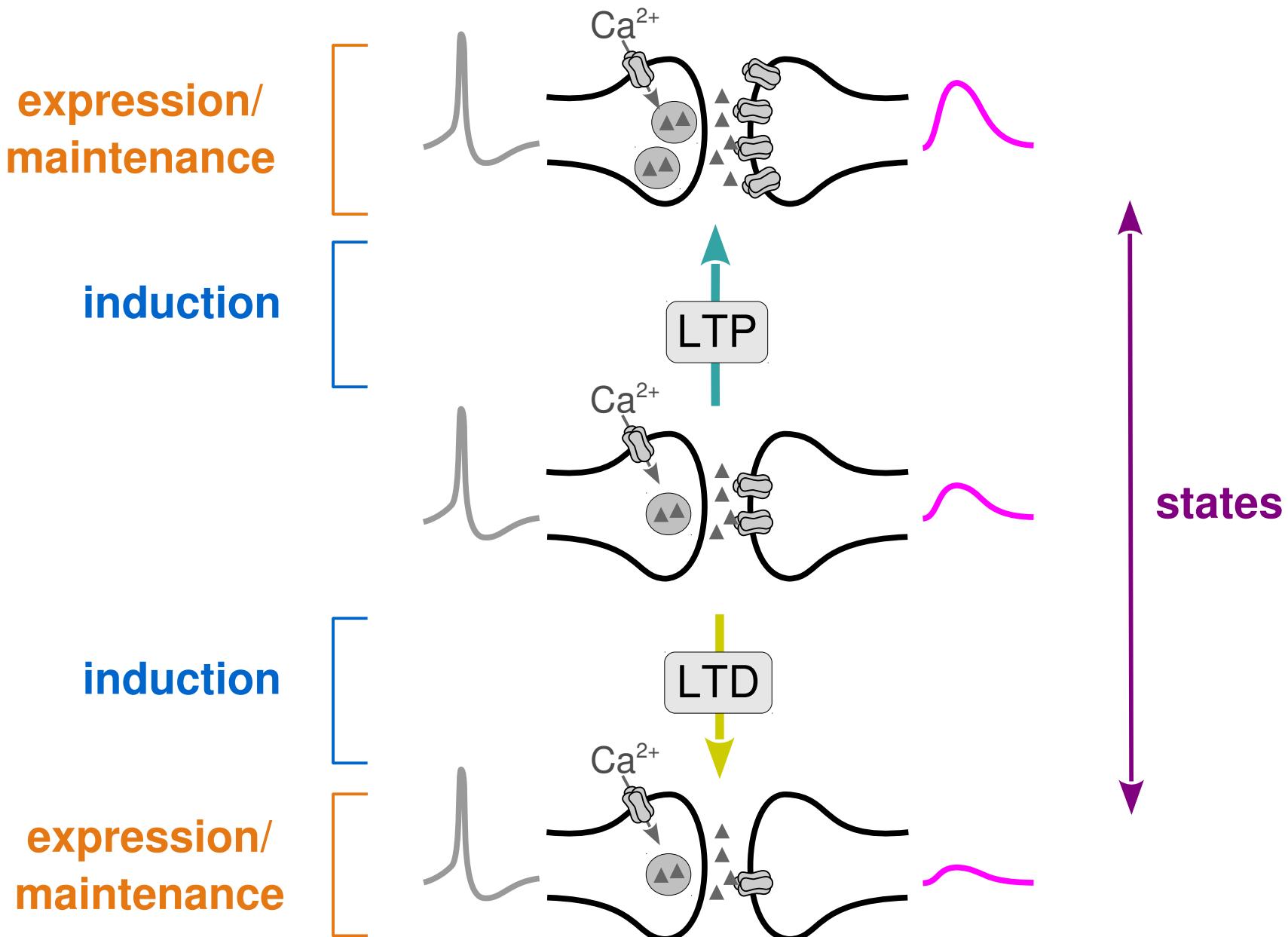
- transient change in transmission efficacy
- time scale of changes  $\sim 1$  sec

# Long-term synaptic plasticity



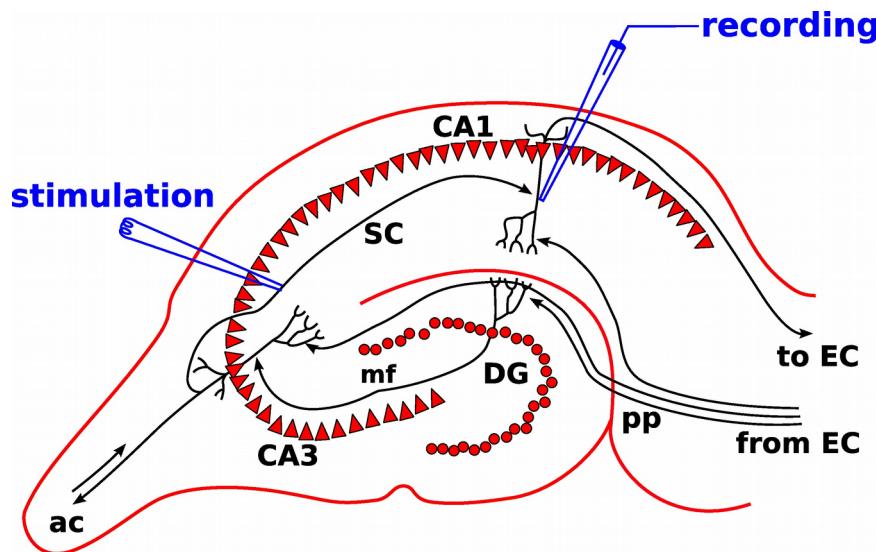
- long-lasting change ( $>60$  min) in transmission efficacy
- time scale of induction ~ 1 min

# Synaptic plasticity: induction, maintenance & states



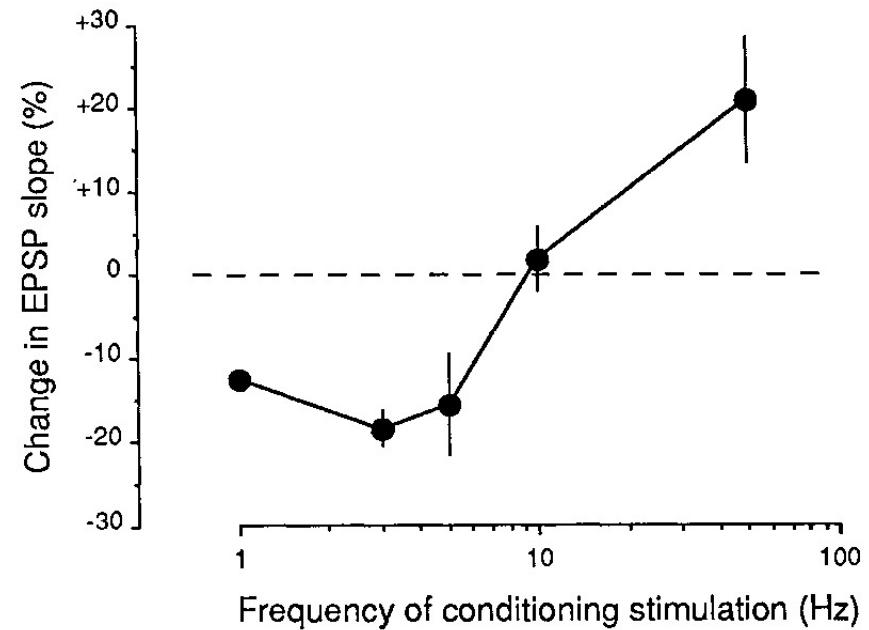
# Plasticity induction: spike-frequency stimulation

hippocampus (slices)



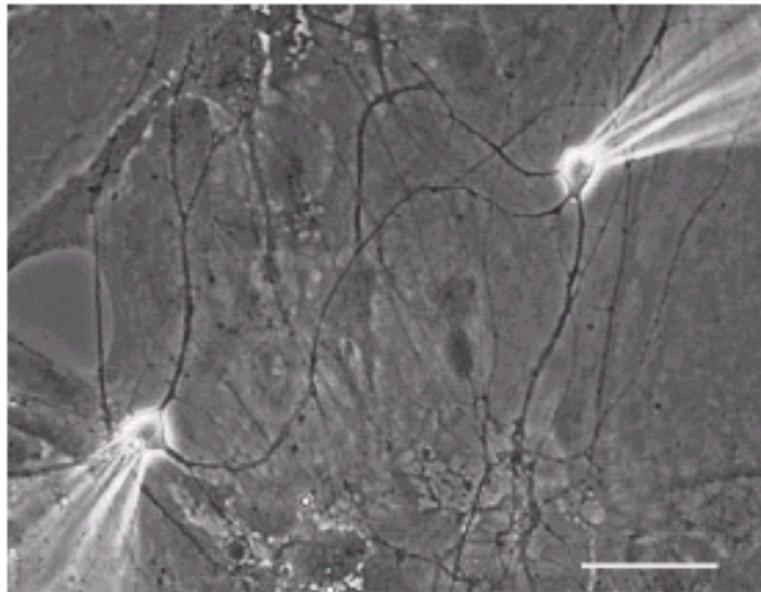
pre post

900 pulses at 1-50 Hz

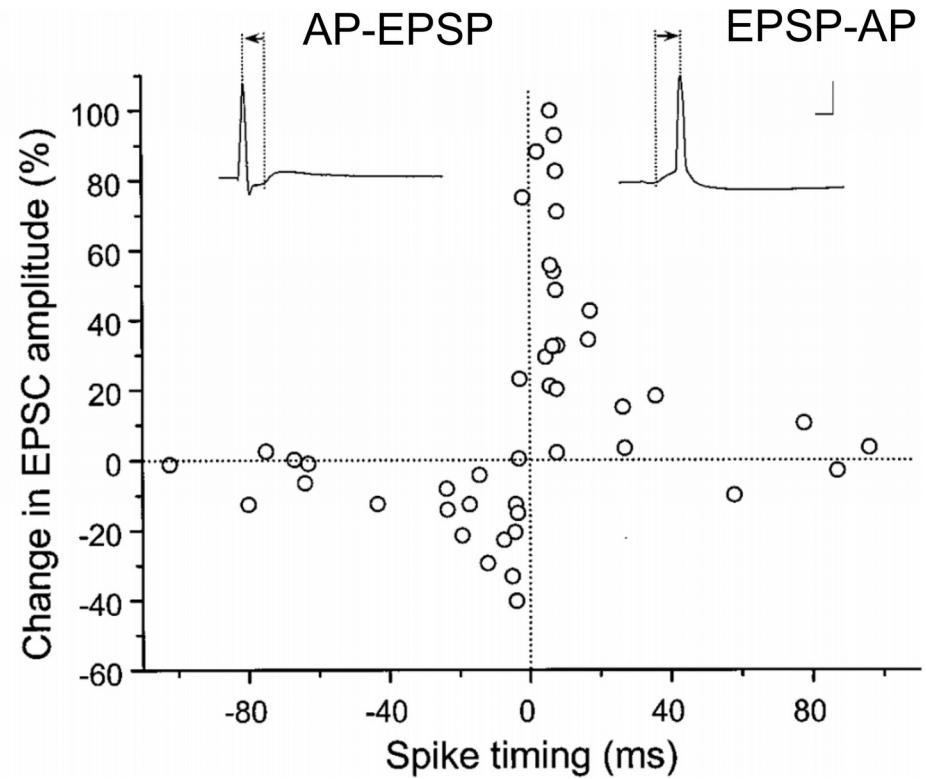
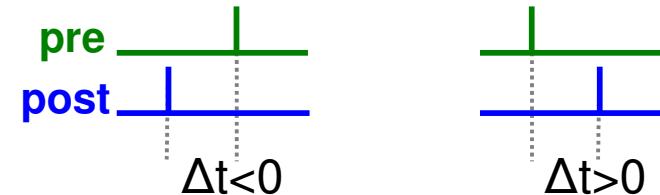


# Plasticity induction : spike-pair stimulation

hippocampal cultures



60 pairings @ 1 Hz

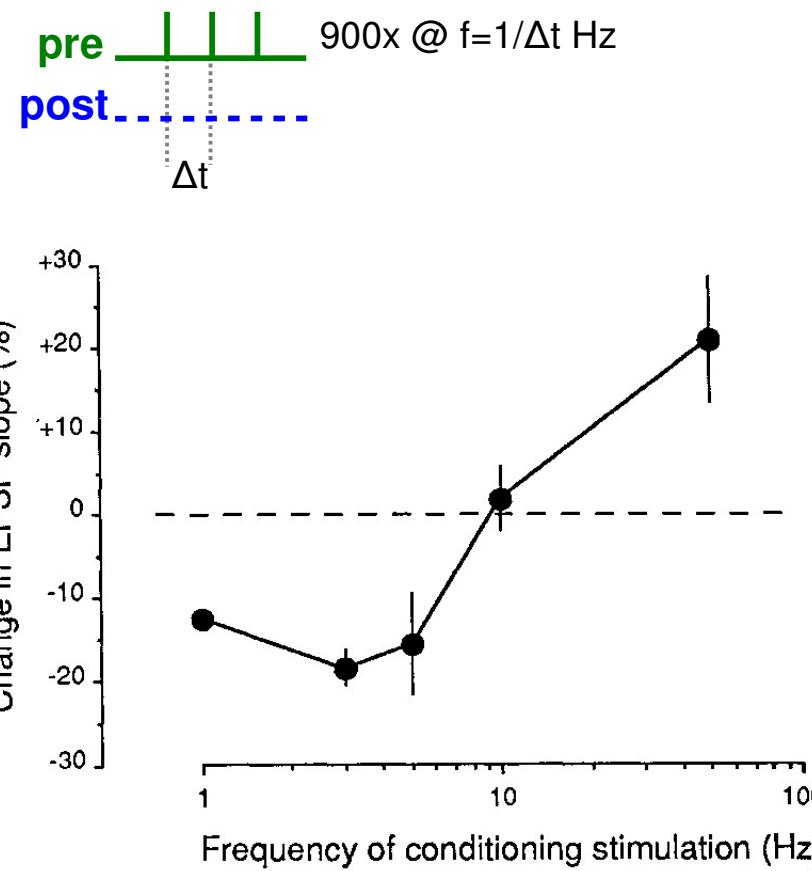


[Bi & Poo, J Neurosci 1998]

[Magee & Johnston 1997; Zhang et al. 1998; Markram et al. 1997; Sjöström et al. 2001; Feldman 200]

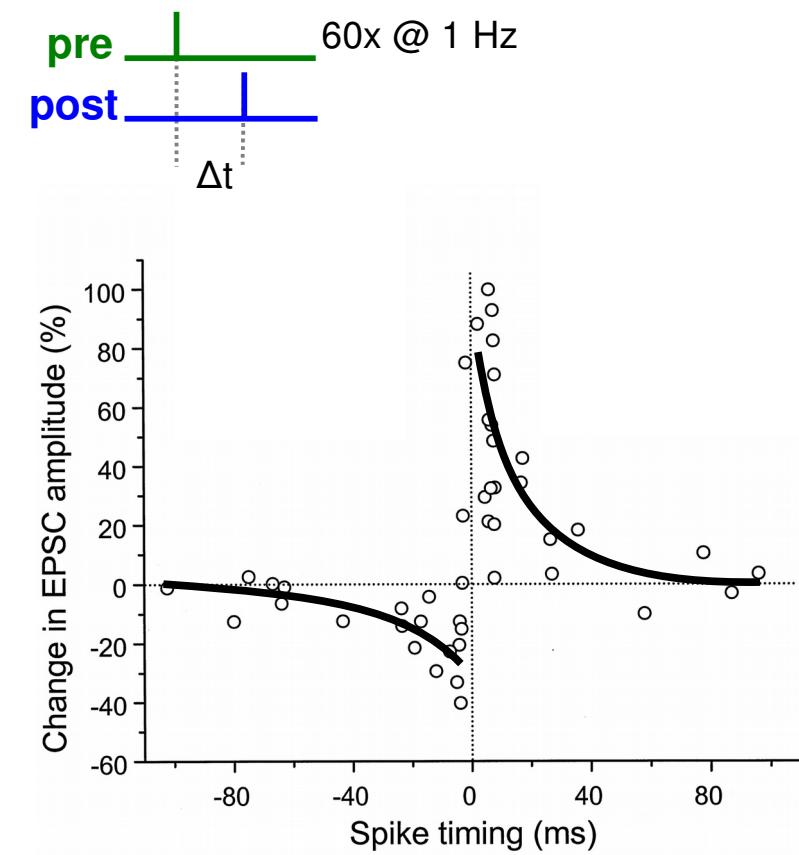
# Induction: Stimulation protocols evoking LTP/LTD

spike-frequency



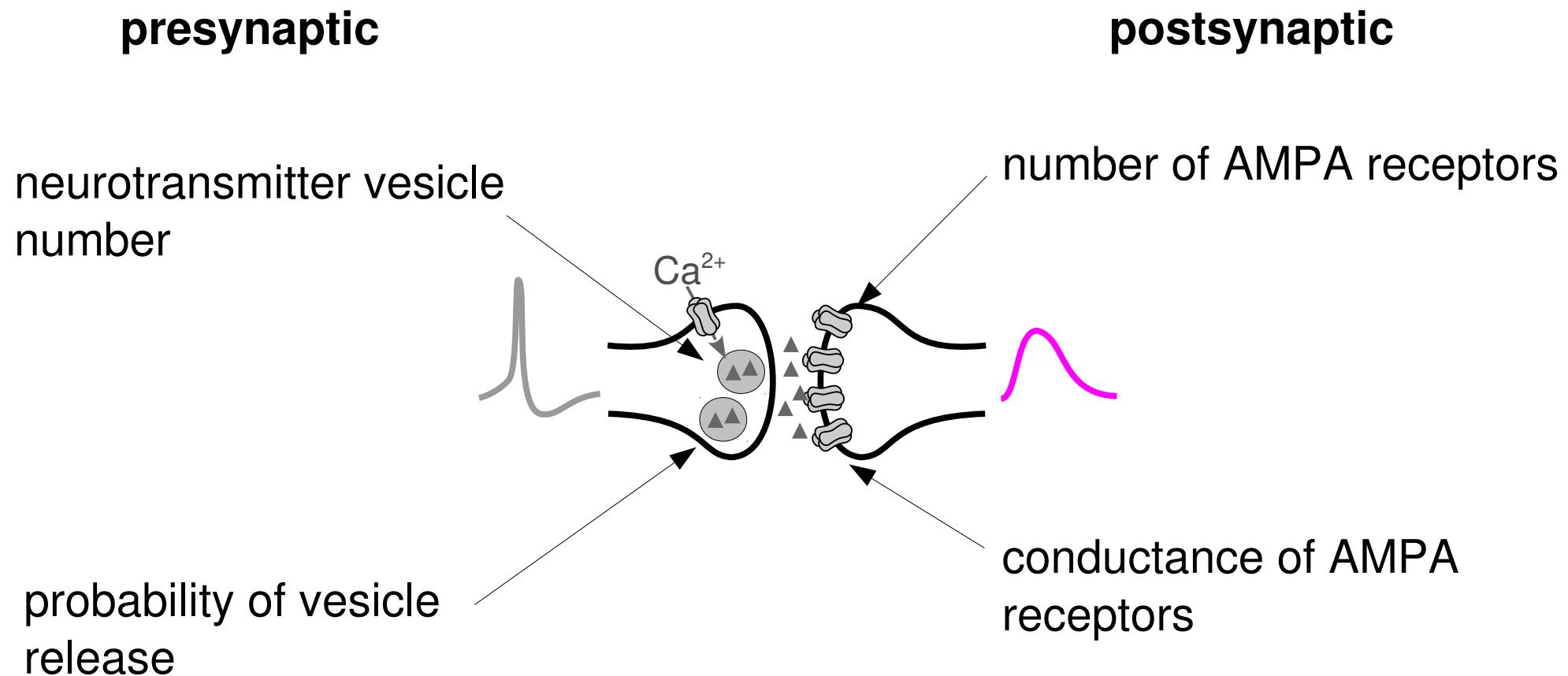
[Dudek *et al.*, 1992]

spike-timing



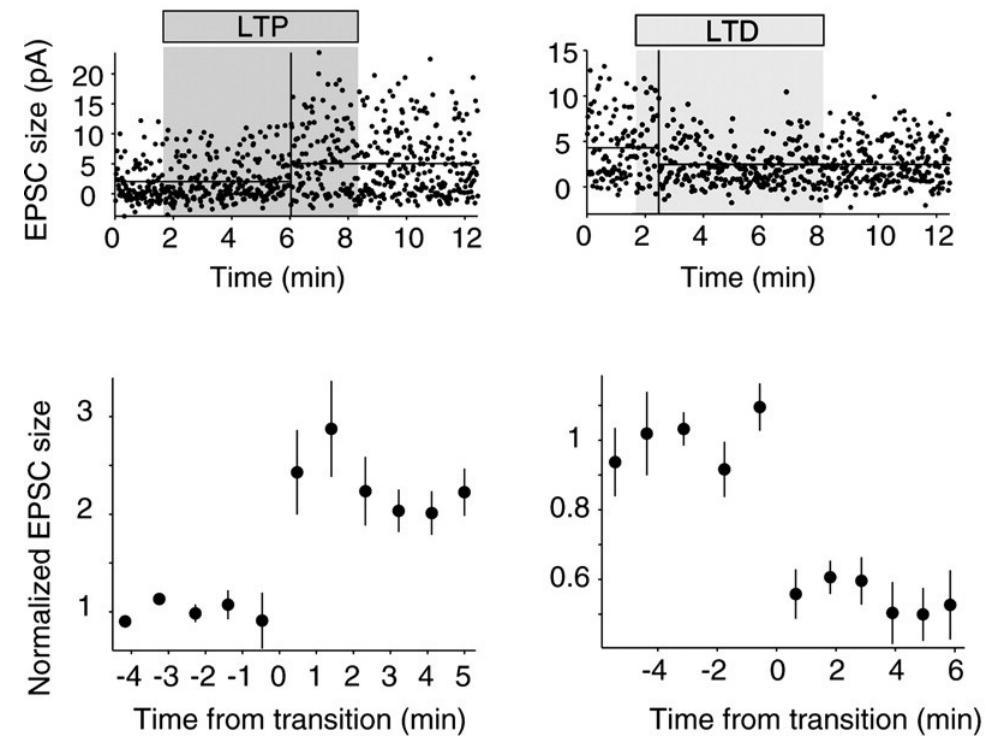
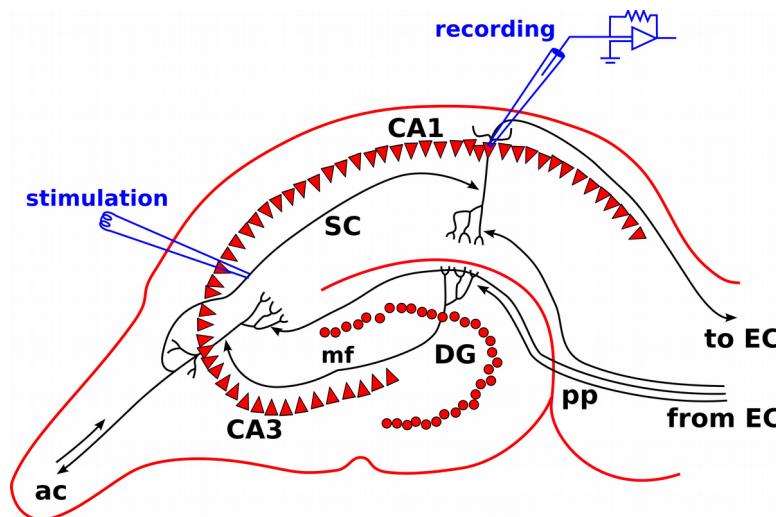
[Bi & Poo, 1998]

# Expression of long-term changes



# States of a synapse : analog or digital?

- most experiments involved multiple synaptic contacts
- Petersen *et al.* 1998, O'Connor *et al.* 2005 investigate single synapse  
→ suggest binary synapse



[O'Connor *et al.*, 2005]

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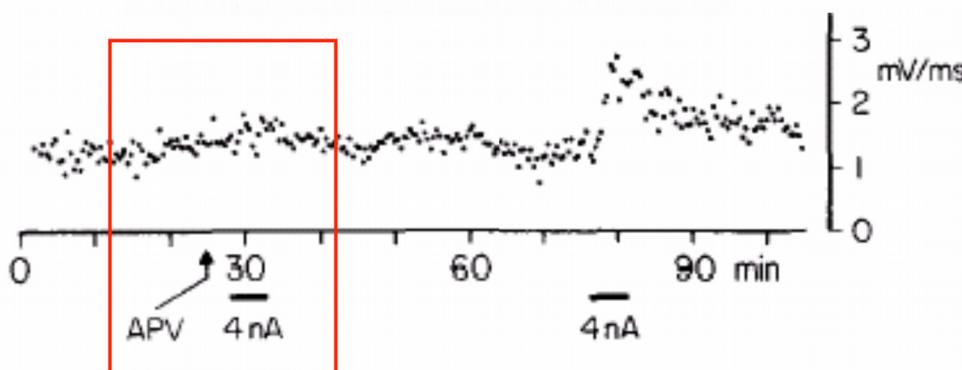
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3.1 Calcium-control hypothesis

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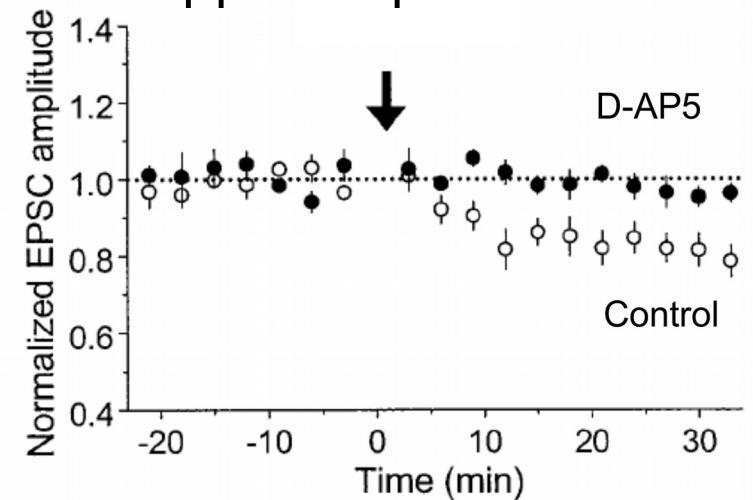
# Plasticity requires NMDA receptor activation

hippocampal slices



[Gustafsson et al. *J Neurosci* 1987]

hippocampal cultures

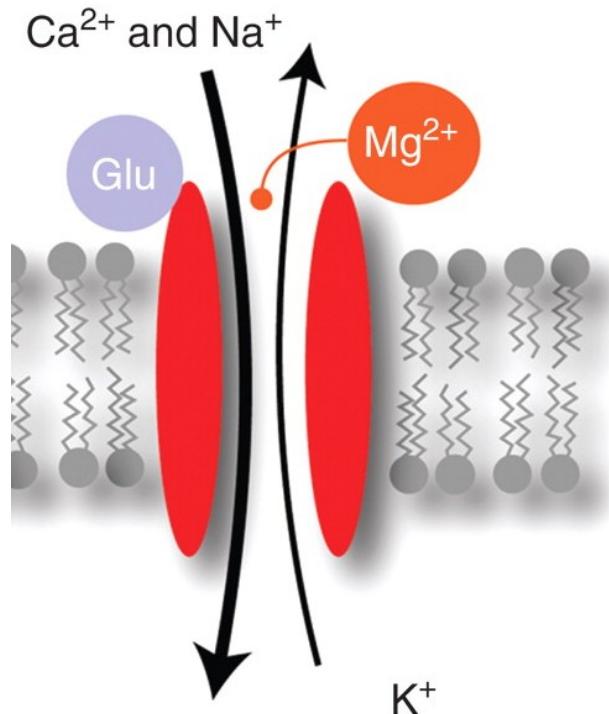


[Bi & Poo *J Neurosci* 1998]

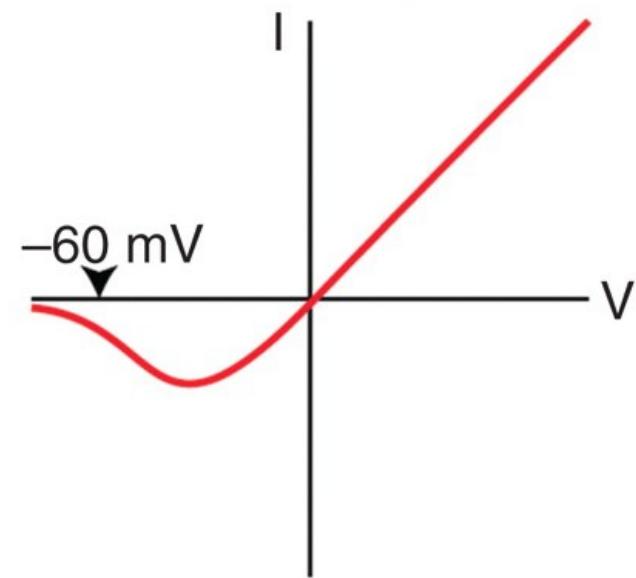
## NMDAR antagonist blocks LTP/LTD induction

- CA3-CA1 pyramidal cell synapse
- CA3-CA3 pyramidal cell synapse
- Layer V – layer V synapse
- Layer II/III
- Layer IV stellate cell synapse
- Dorsal cochlear neurons (brainstem)
- Retino-tectal synapse

# Induction: postsynaptic NMDA receptor activation required

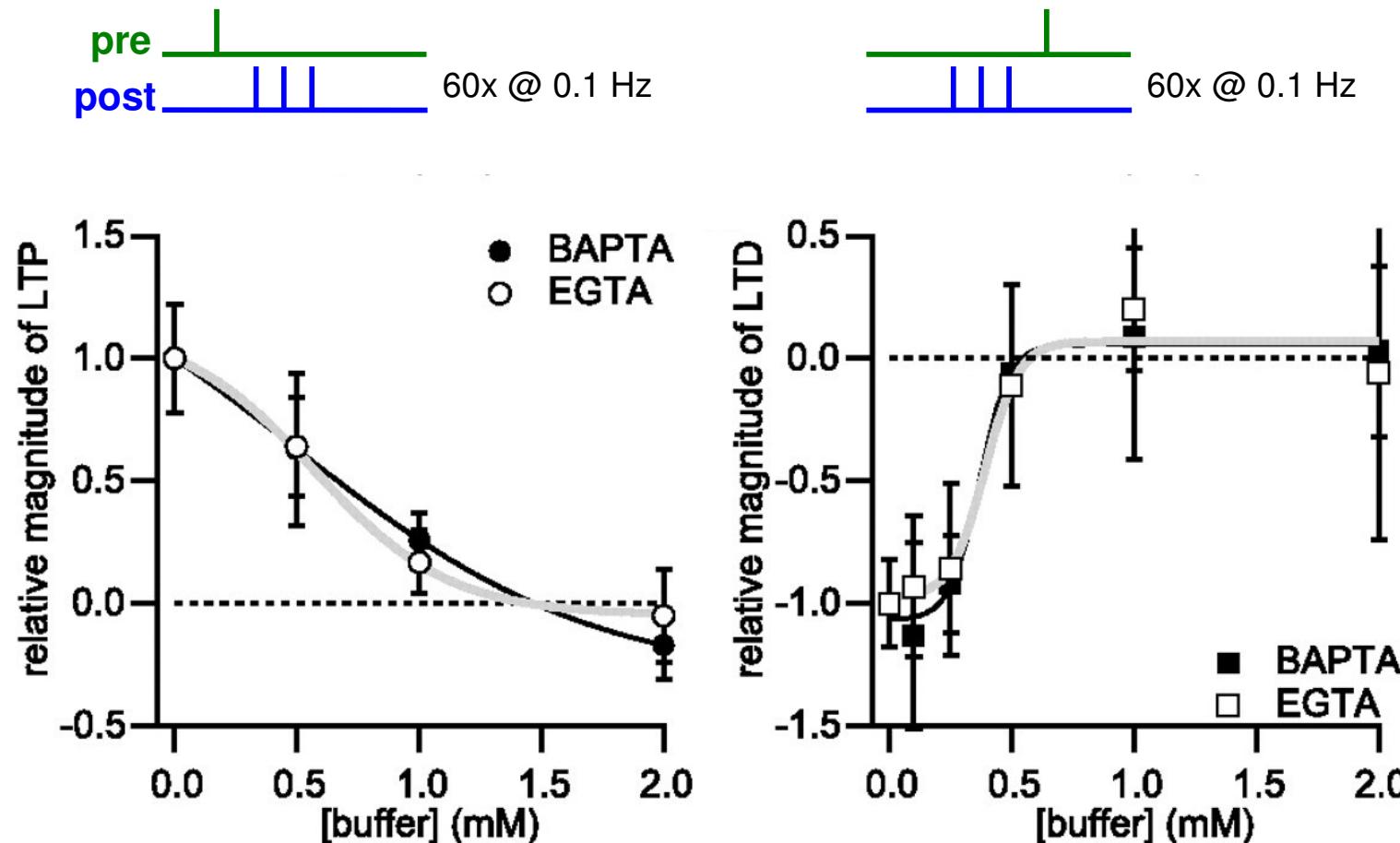


current-voltage relationship



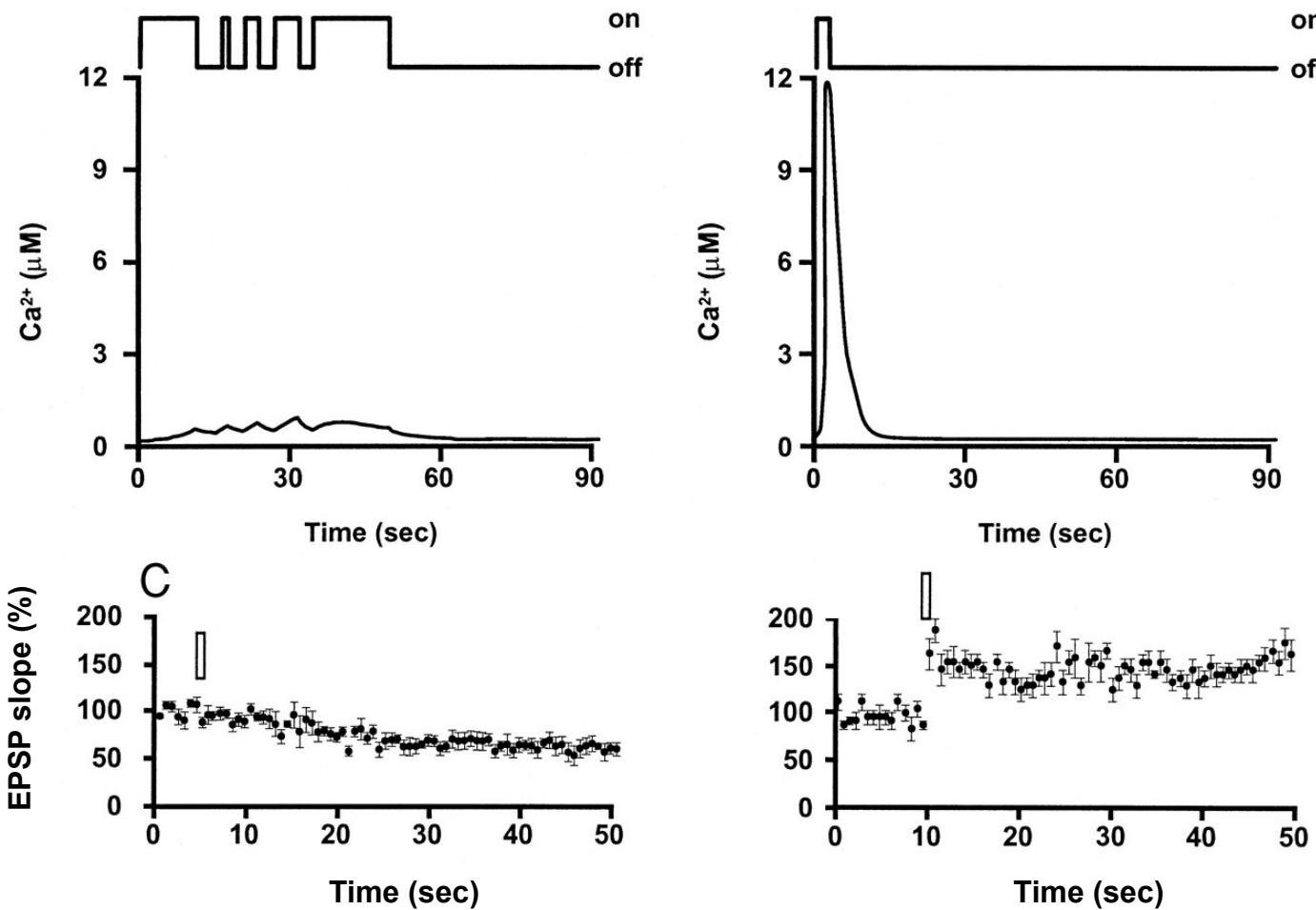
- coincidence detector :
  - presynaptic action potential → glutamate (Glu)
  - postsynaptic depolarization → Mg<sup>2+</sup> block is expelled
- calcium permeable

# Postsynaptic calcium required for plasticity

[Nevian & Sakmann *et al.*, 2006]

[Lynch *et al.*, 1983; Malenka *et al.*, 1988; Neveu and Zucker, 1996; Yang *et al.*, 1999; Zucker, 1999; Mizuno *et al.*, 2001; Ismailov *et al.*, 2004]

# Postsynaptic calcium sufficient for plasticity

[Yang *et al.*, 1999]

- LTP induced by brief, large amplitude  $[\text{Ca}^{2+}]$  increases
- prolonged, modest rise in  $[\text{Ca}^{2+}]$  elicits LTD

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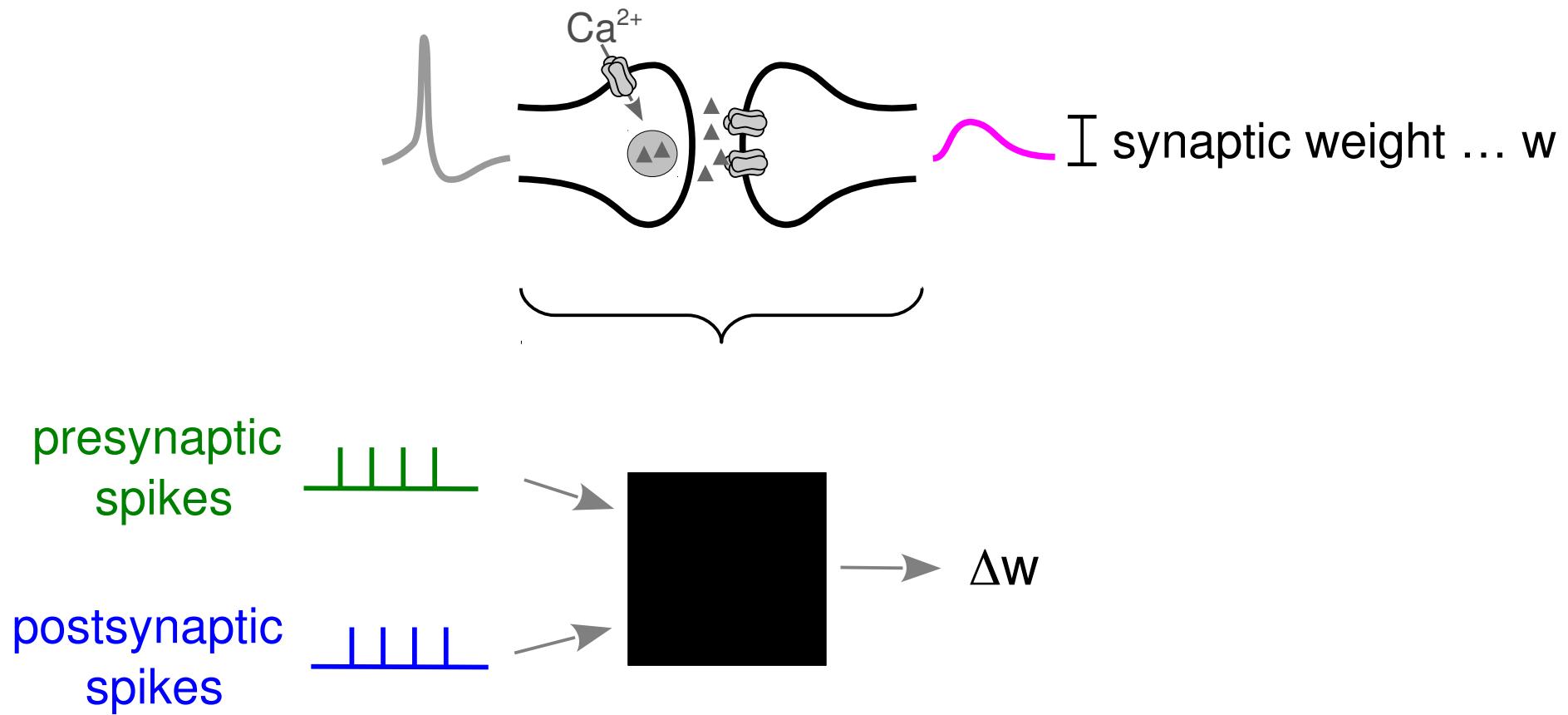
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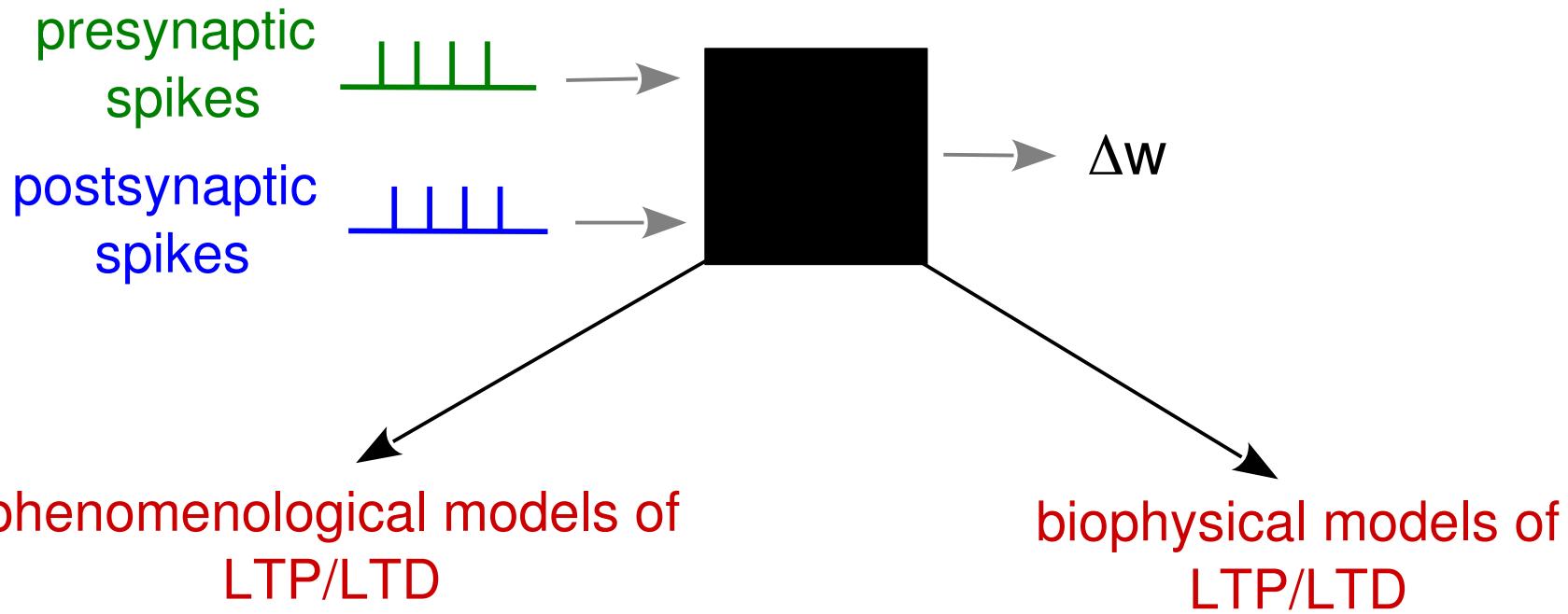
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### 3. Biophysical models of synaptic plasticity

## Plasticity models link activity to synaptic change



# Modeling approaches : phenomenological vs. biophysical



- use pre- and postsynaptic spike times or rate to calculate change in synaptic strength
- conversion can involve arbitrarily complex mathematical models
- resolve *parts* of the underlying biological machinery involved in the induction of plasticity
- degree of biological detail varies largely

# Modeling studies : phenomenological vs. biophysical

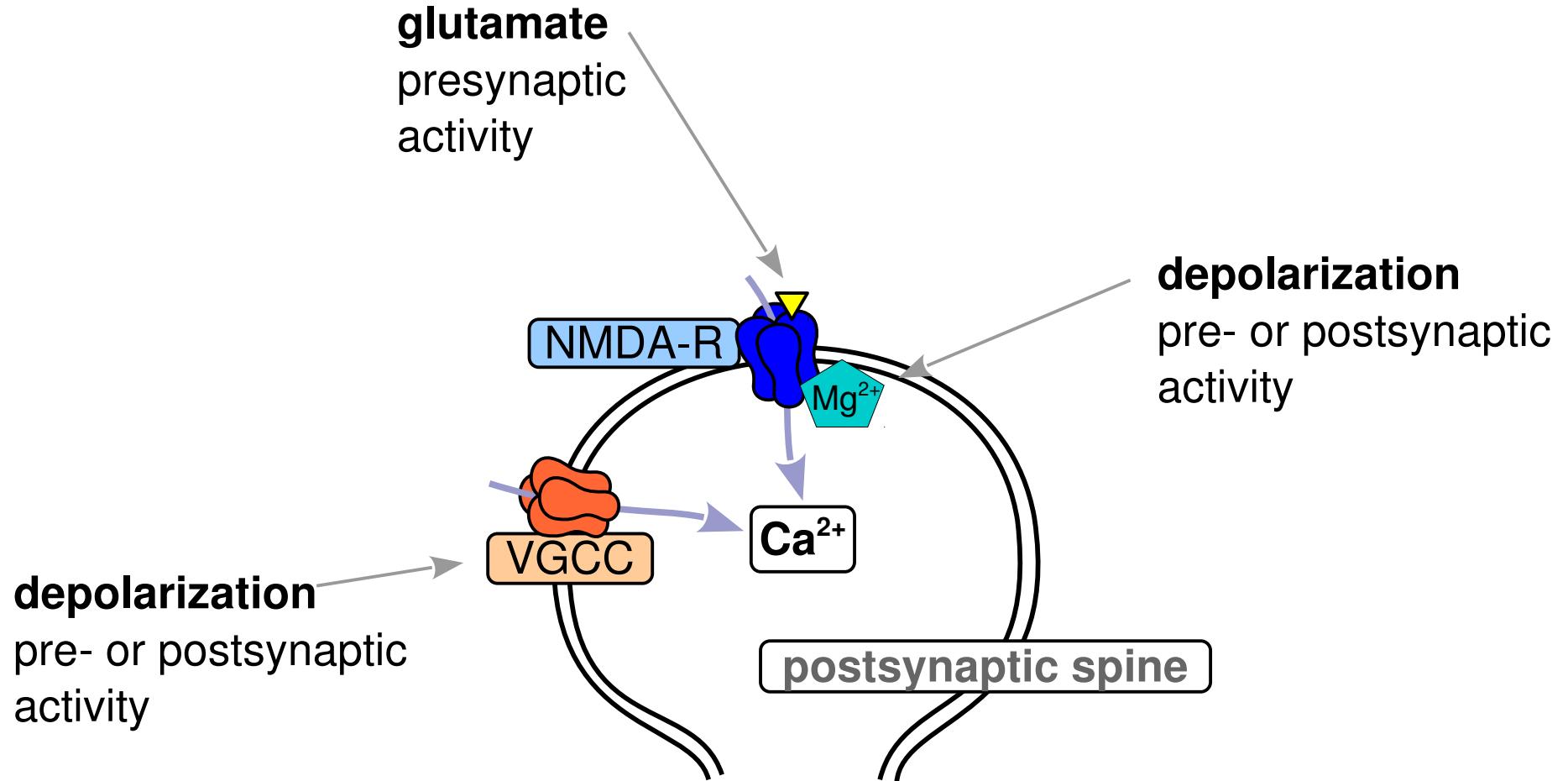
## phenomenological models of LTP/LTD

- **rate-based plasticity models**  
[Hebb, 1949; Bienenstock *et al.*, 1982;  
Oja, 1982]
- **spike-timing based models**  
[Gerstner *et al.*, 1996; van Rossum *et al.* 2000;  
Song, 2000; Pfister & Gerstner, 2006]

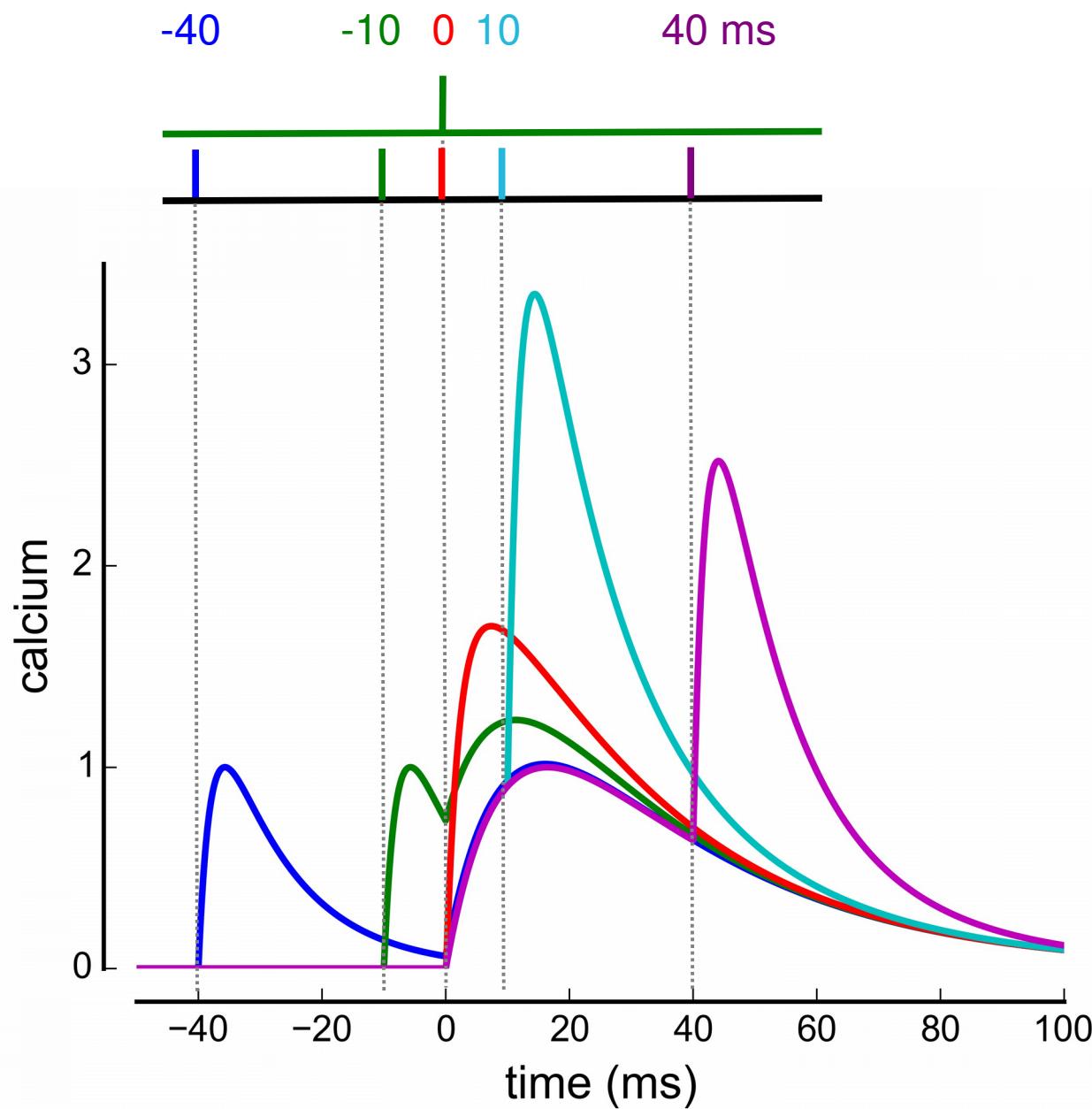
## biophysical models of LTP/LTD

- **Voltage-based models**  
[Clopath *et al.* 2010]
- **$\text{Ca}^{2+}$  – dynamics based models**  
[Karmarkar *et al.*, 2002; Shouval *et al.*, 2002;  
Rubin *et al.*, 2005; Graupner *et al.* 2012]
- **CaMKII kinase-phosphatase system**  
[Crick 1984; Lisman, 1985;  
Okamoto & Ichikawa, 2000; Zhabotinsky, 2000;  
Graupner & Brunel, 2007; Urakubo *et al.*, 2008]
- **extensive protein networks**  
[Bhalla & Iyengar, 1999; Hayer & Bhalla, 2005]
- **local clustering of receptors**  
[Shouval, 2005]

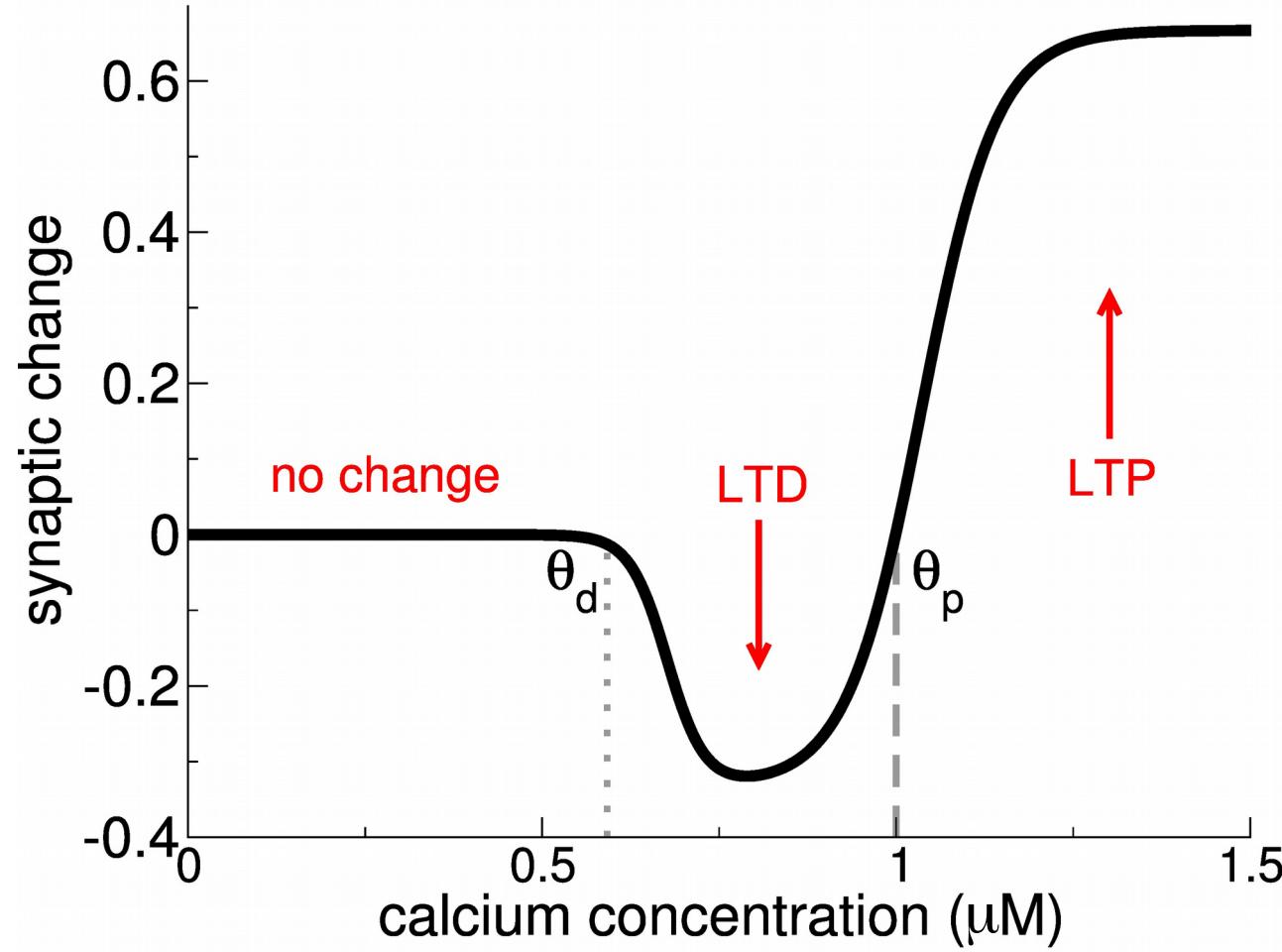
# Calcium influx



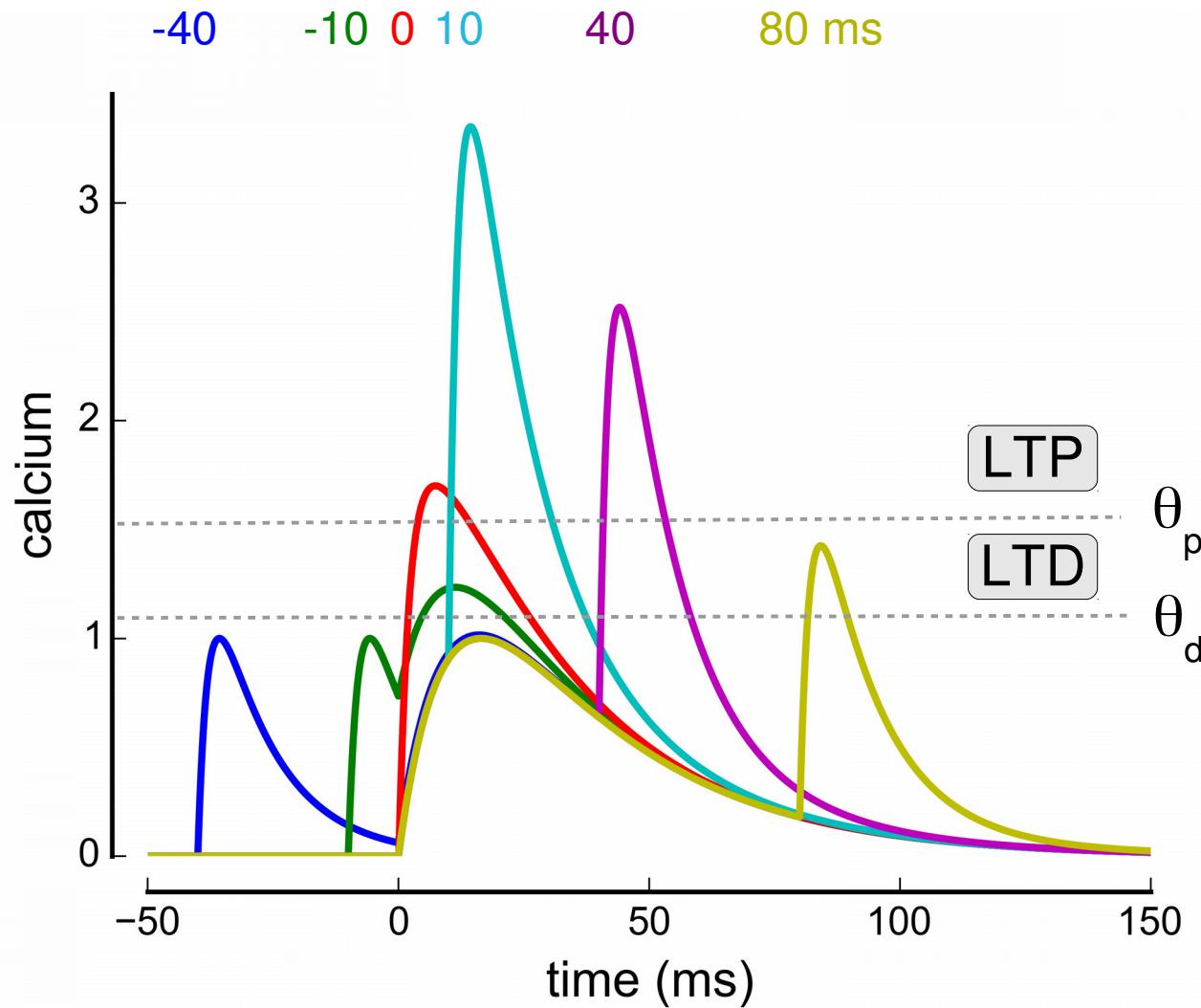
# Calcium transients from spike-pair stimulation



# Calcium control hypothesis

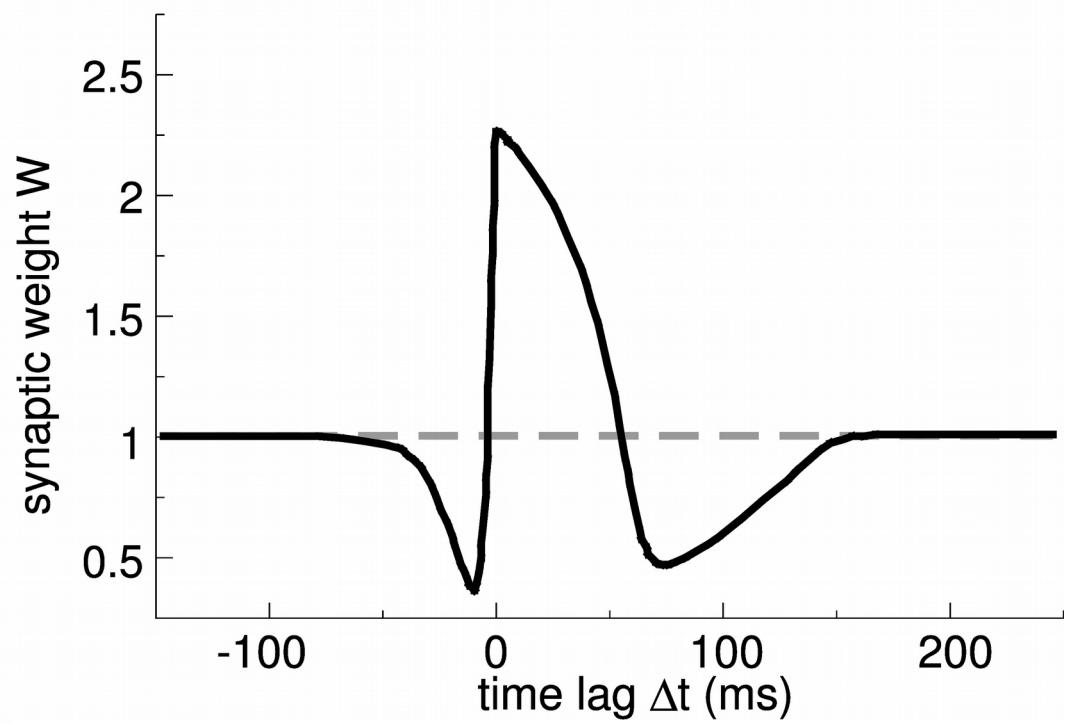
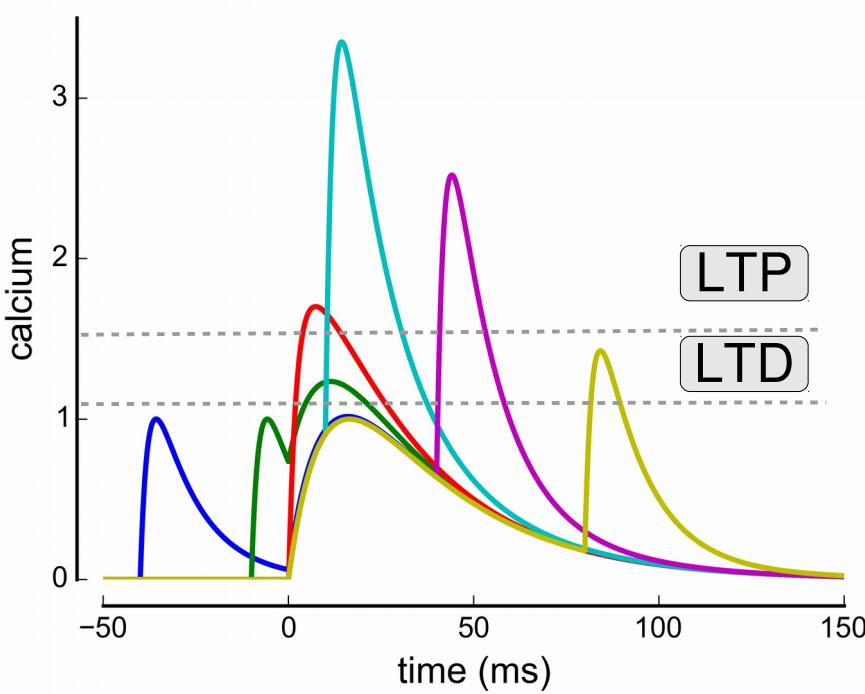
[Shouval *et al.*, 2002]

# Calcium transients from spike-pair stimulation



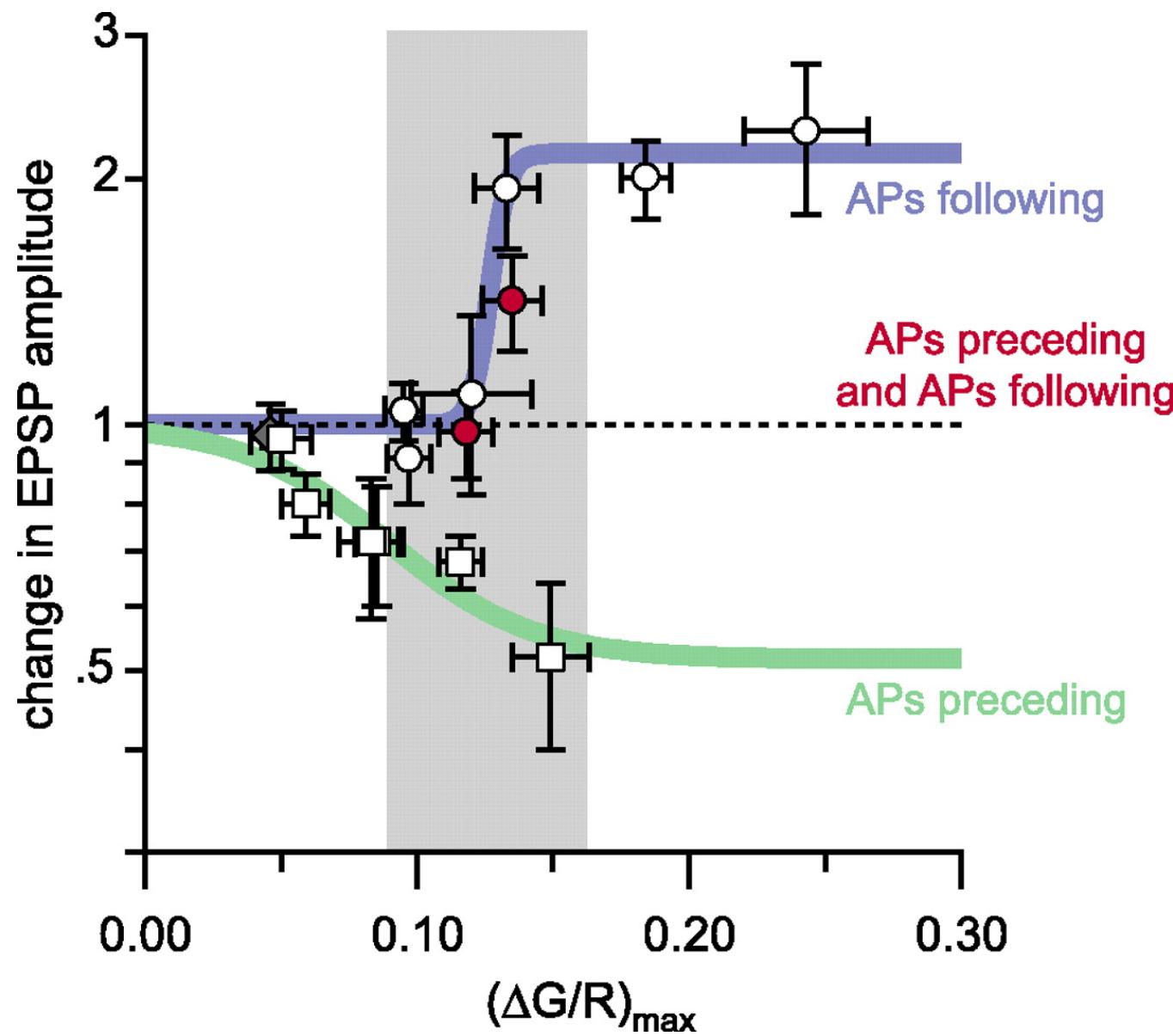
### 3. Biophysical models of synaptic plasticity

## STDP curve



[Shouval *et al.*, 2002]

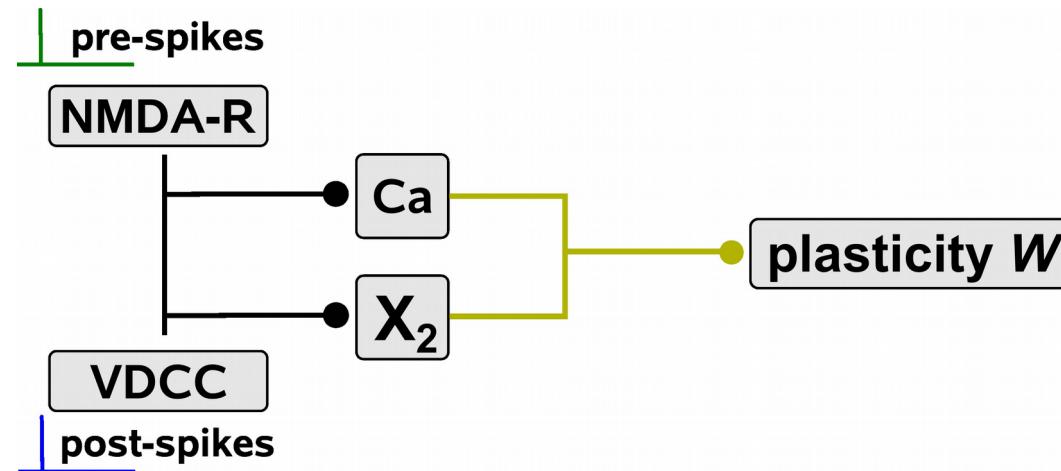
# Peak $\text{Ca}^{2+}$ amplitude does not predict LTP or LTD

[Nevian & Sakmann *et al.*, 2006]

### 3. Biophysical models of synaptic plasticity

## More complex read-out mechanisms of $\text{Ca}^{2+}$ signal

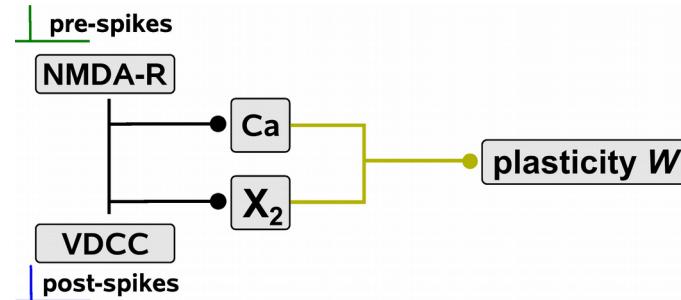
- two distinct but converging dynamical variables [Karmarkar *et al.*, 2002; Badoual *et al.*, 2006]



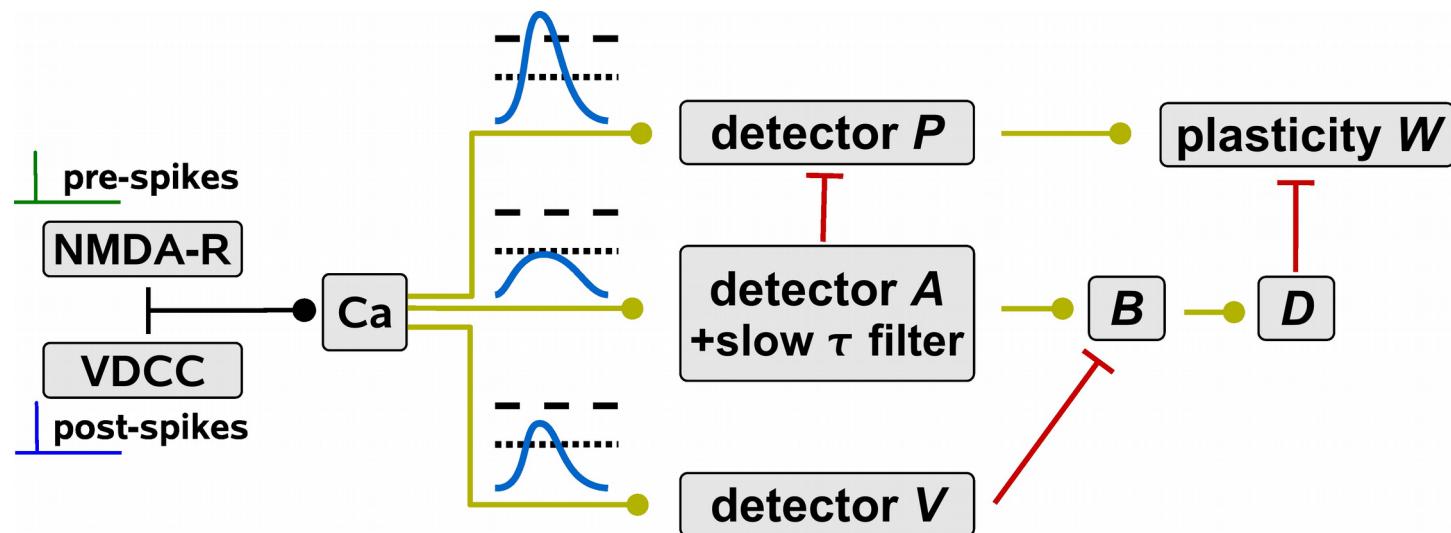
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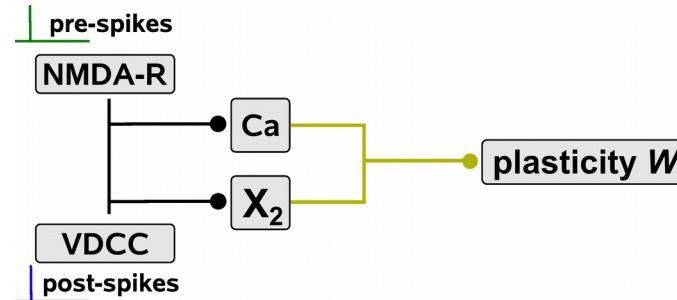
- phenomenological read-out of  $[Ca^{2+}]$  [Rubin *et al.*, 2005]



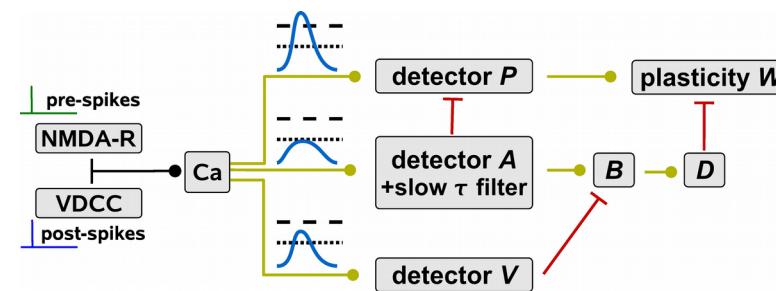
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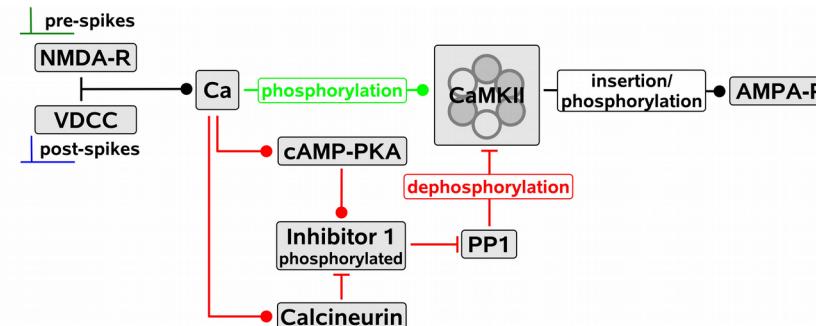
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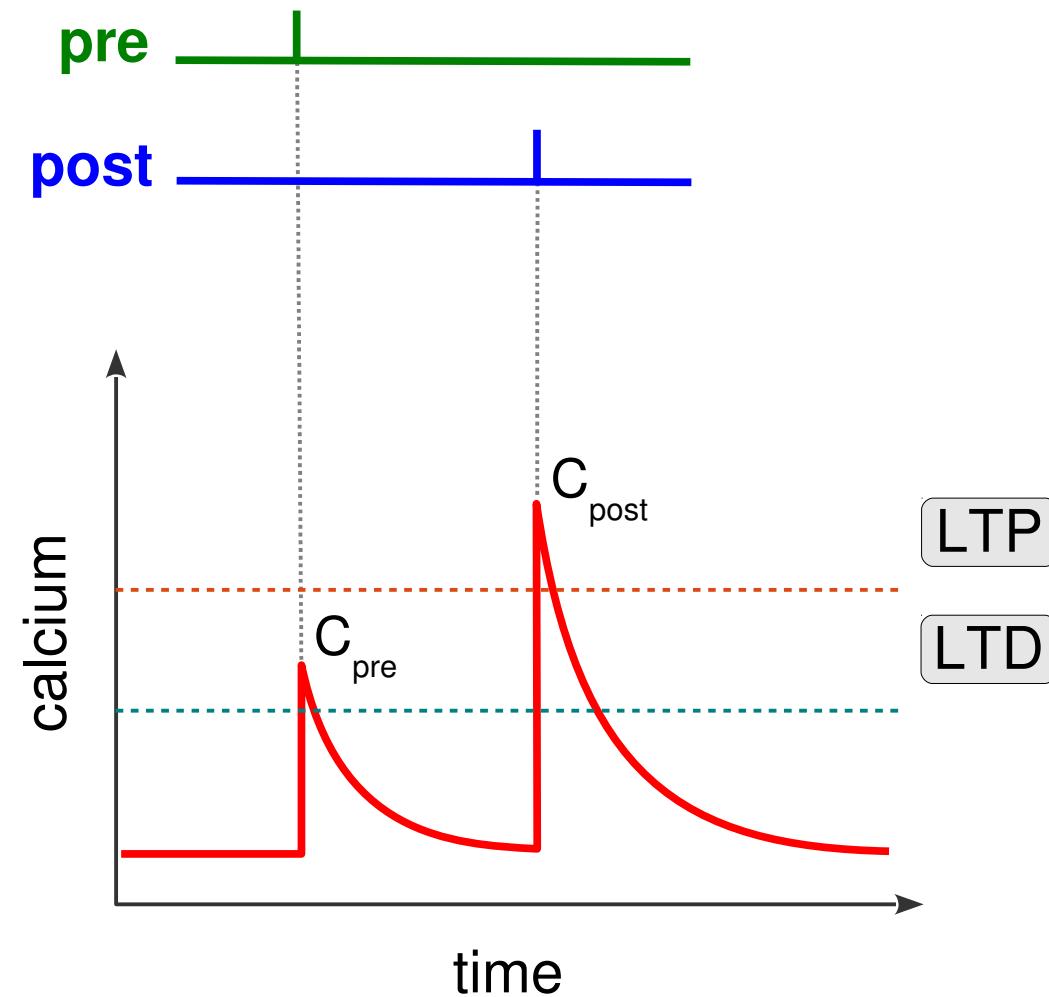


- protein signaling cascade activated by  $[Ca^{2+}]$  [Graupner & Brunel, 2007; Urakubo *et al.*, 2008]



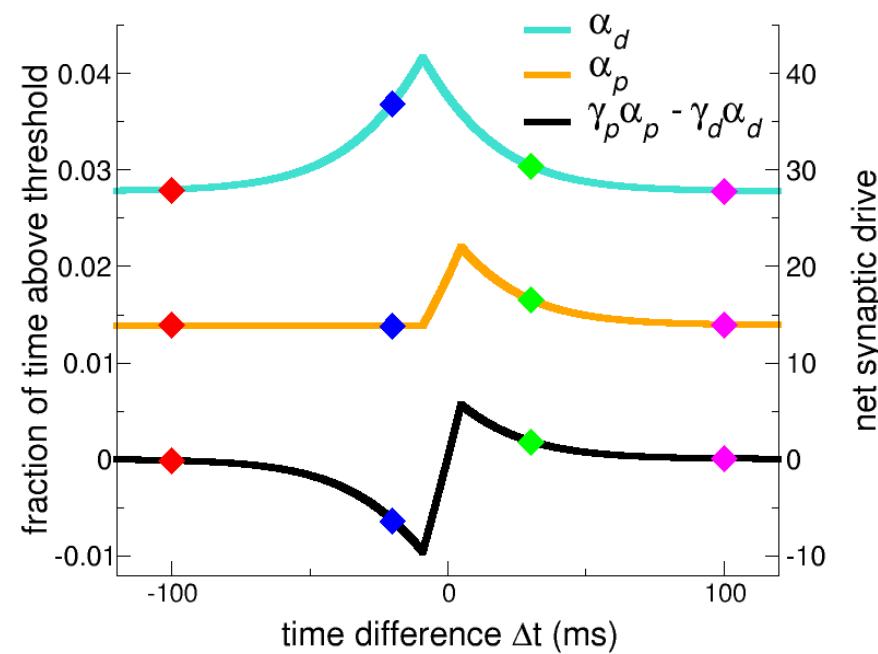
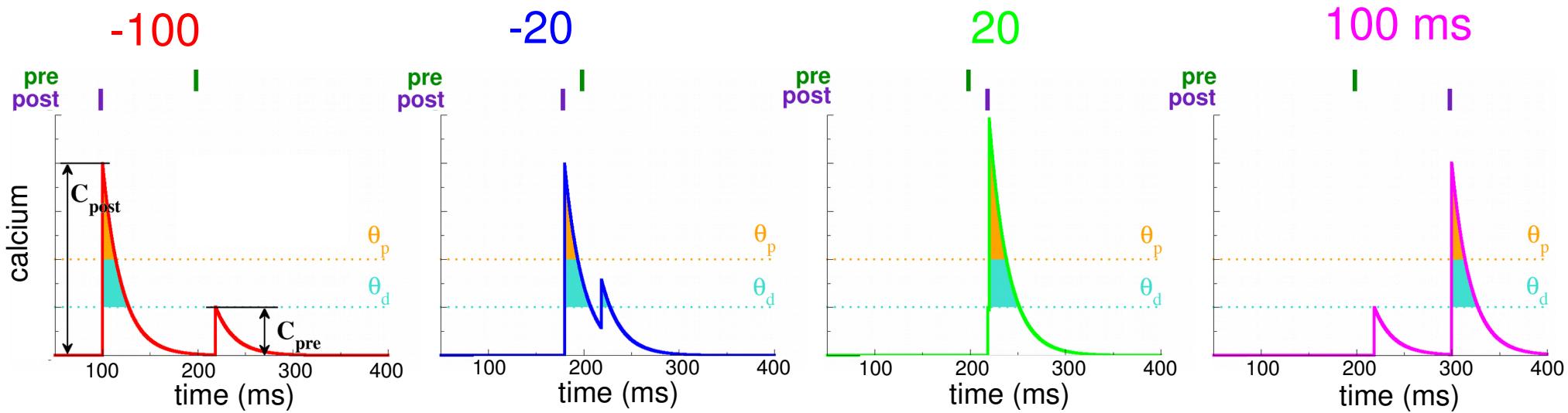
### 3. Biophysical models of synaptic plasticity

## Simplified calcium model



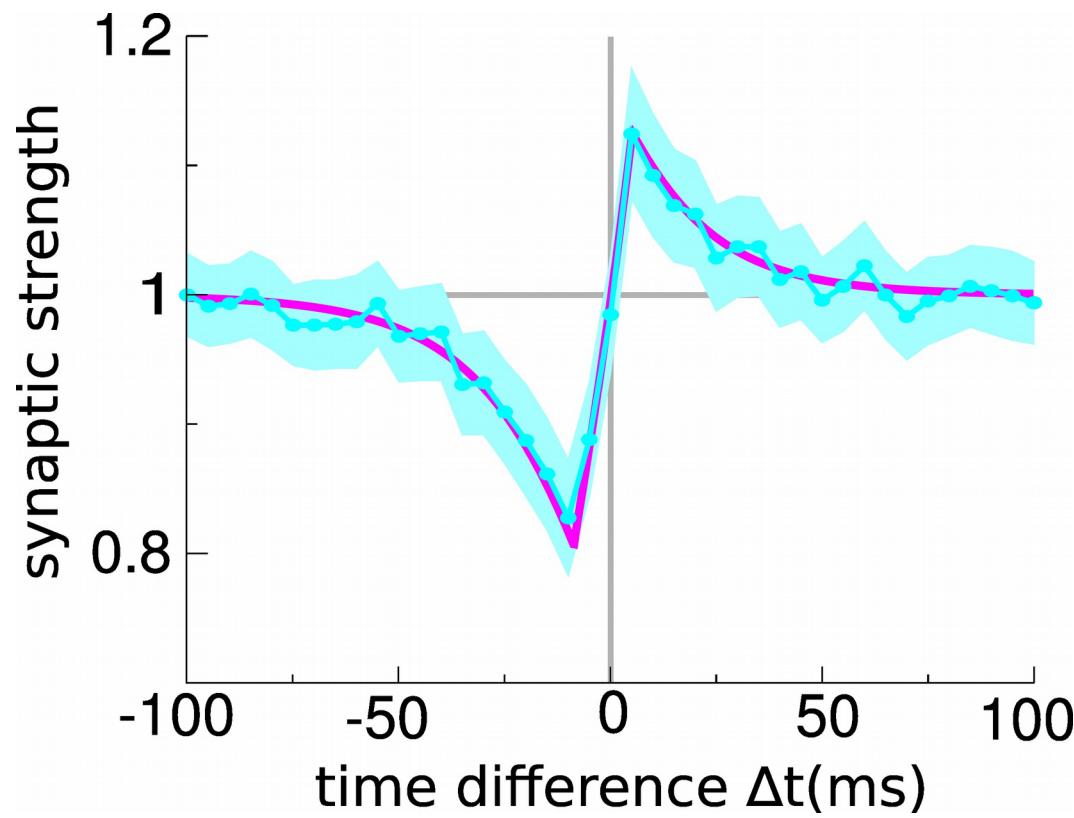
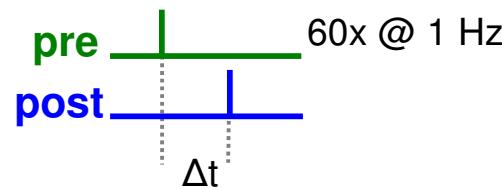
### 3. Biophysical models of synaptic plasticity

## Calcium induced changes : spike-pair stimulation

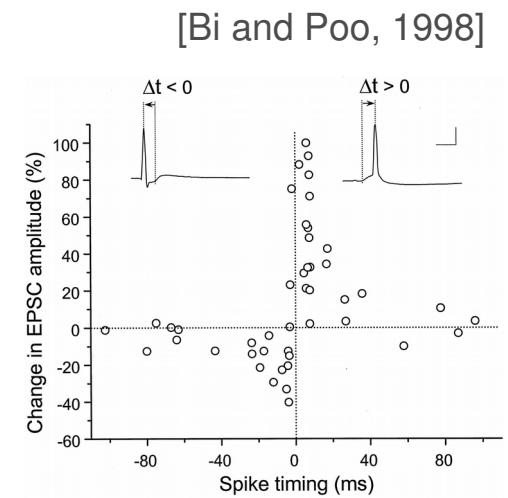


### 3. Biophysical models of synaptic plasticity

## STDP curve in response to spike-pair stimulation

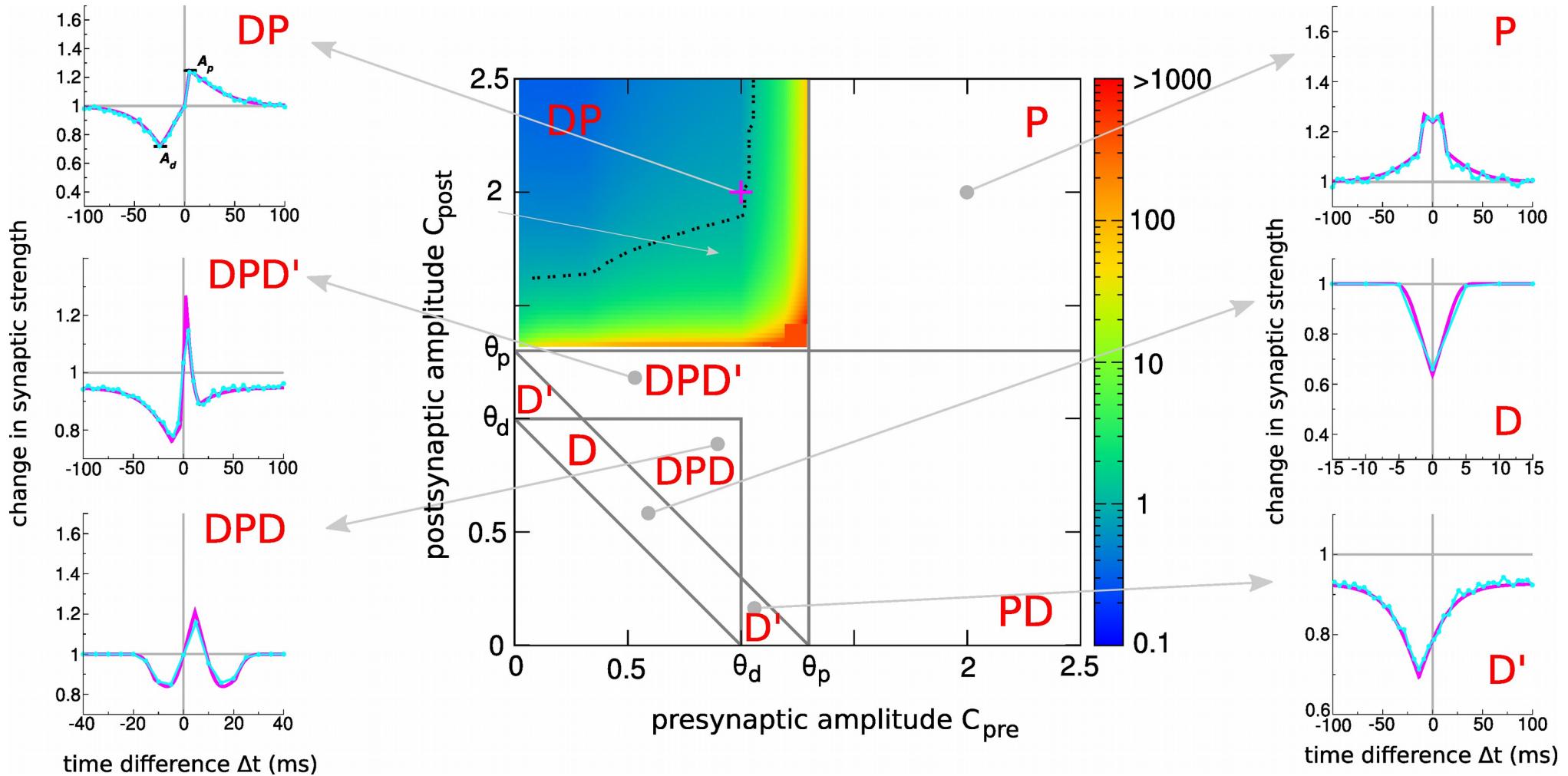


[Graupner & Brunel, 2012]



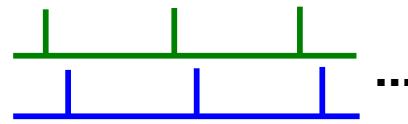
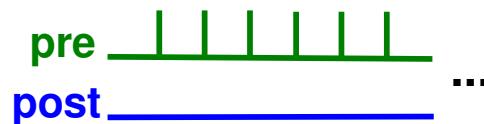
### 3. Biophysical models of synaptic plasticity

## Diversity of STDP curves : spike-pair stimulation

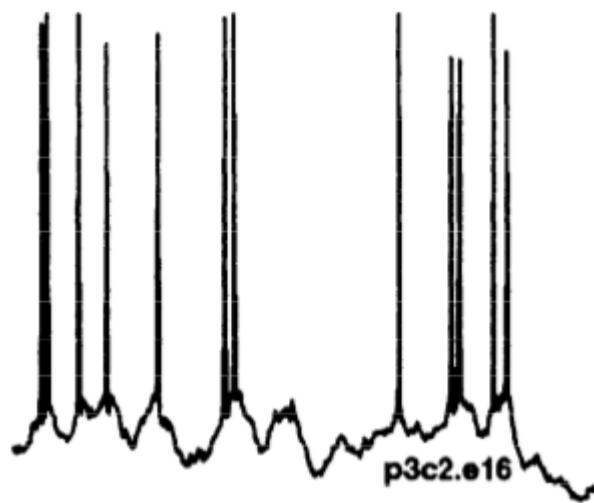


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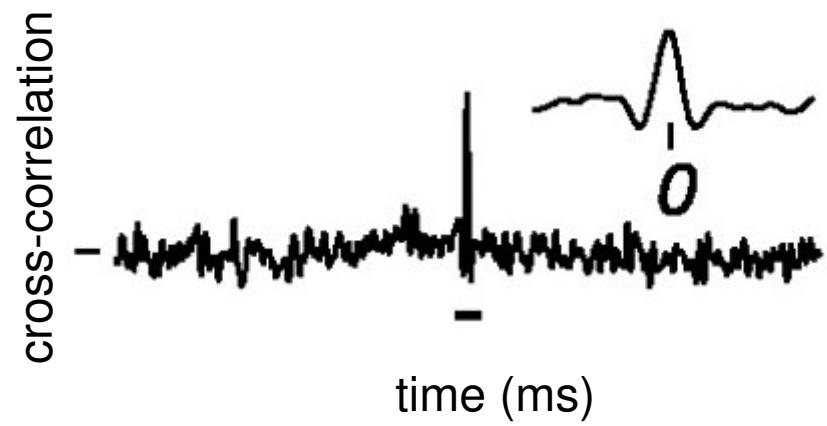
## Plasticity *in vivo* : Realistic firing is highly irregular



In Vivo Visual Stimulation



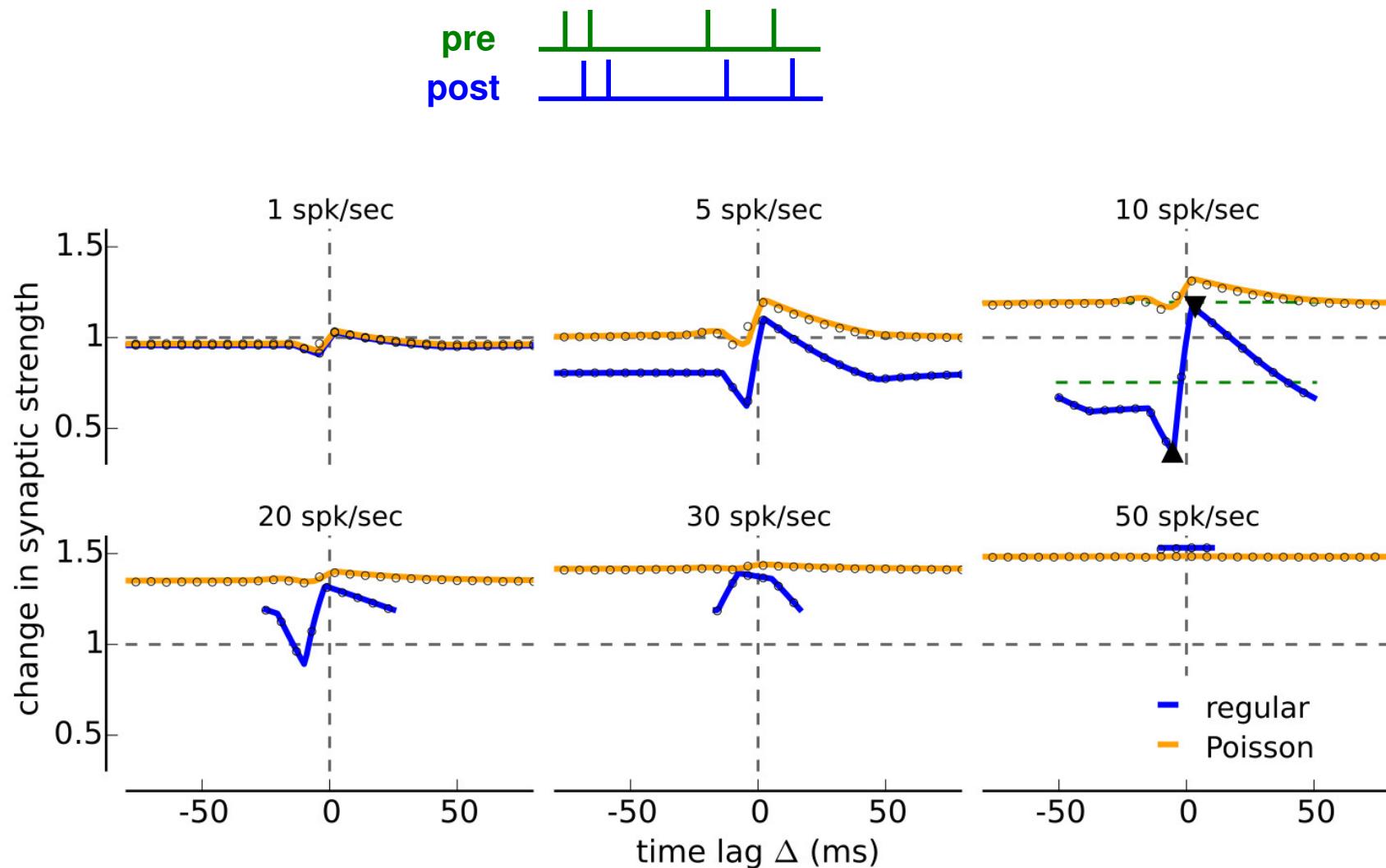
[Holt *et al.*, 1996]



[Kohn and Smith, 2005]

### 3. Biophysical models of synaptic plasticity

## Irregular spike-pairs flatten STDP curve



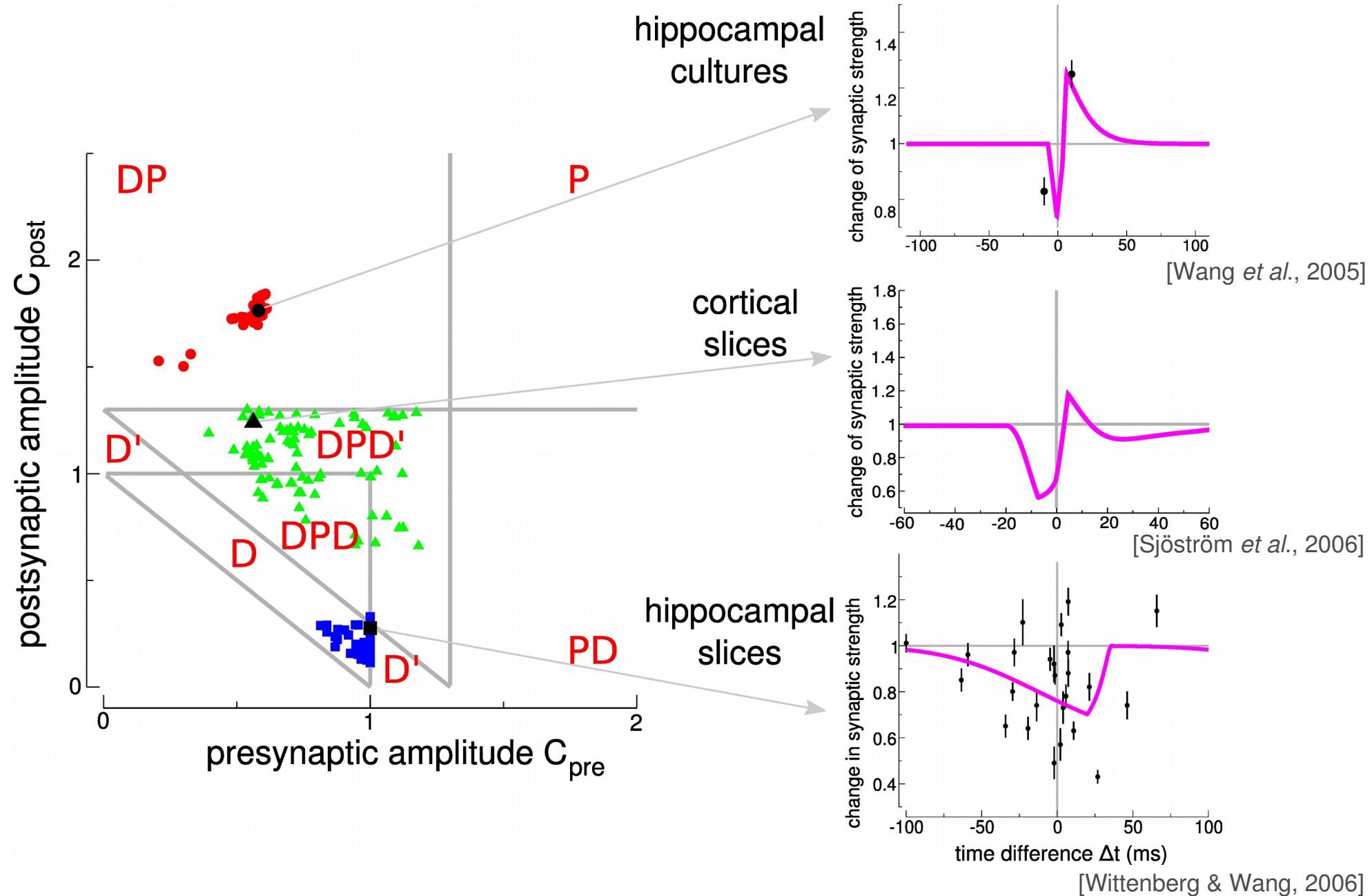
[Graupner et al. *unpublished*]

# Summary

- synapses can change their transmission efficacy in an activity-dependent manner → LTP / LTD
- induction: coincident pre- and postsynaptic activity lead to calcium influx through NMDA receptors, triggering intracellular signaling cascades
- biophysical model resolve various aspects of the synaptic machinery involved in plasticity induction, e.g. the postsynaptic calcium dynamics
- calcium-based plasticity models can account for many aspects of the experimentally observed plasticity phenomenology.

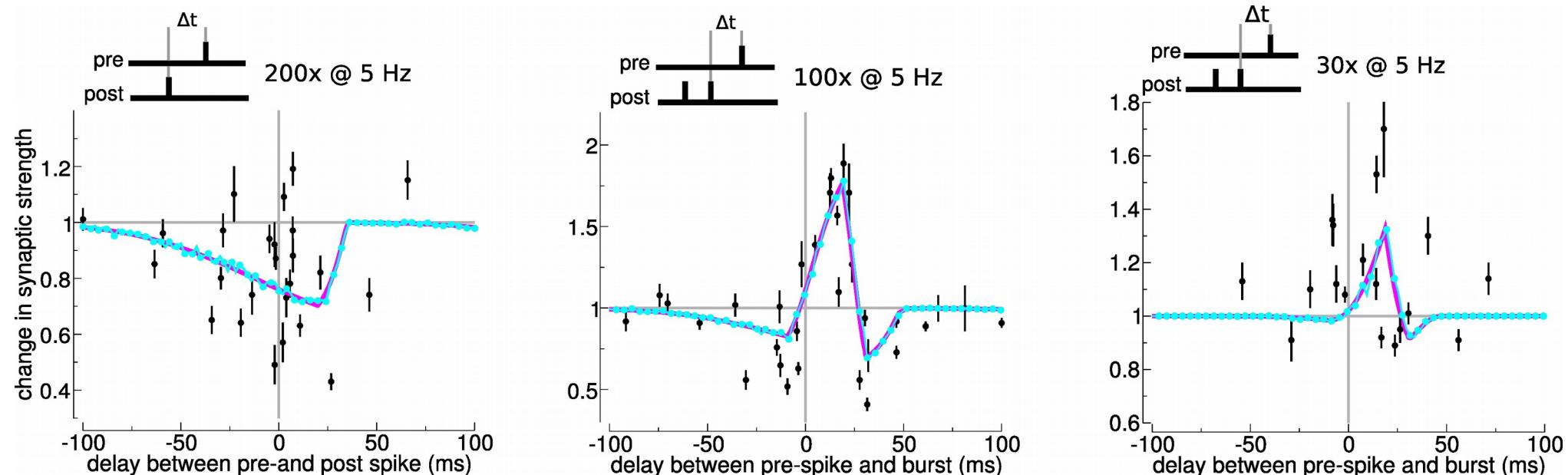
### 3.1 Diversity of plasticity outcomes

## Experiments explained by different parameter sets



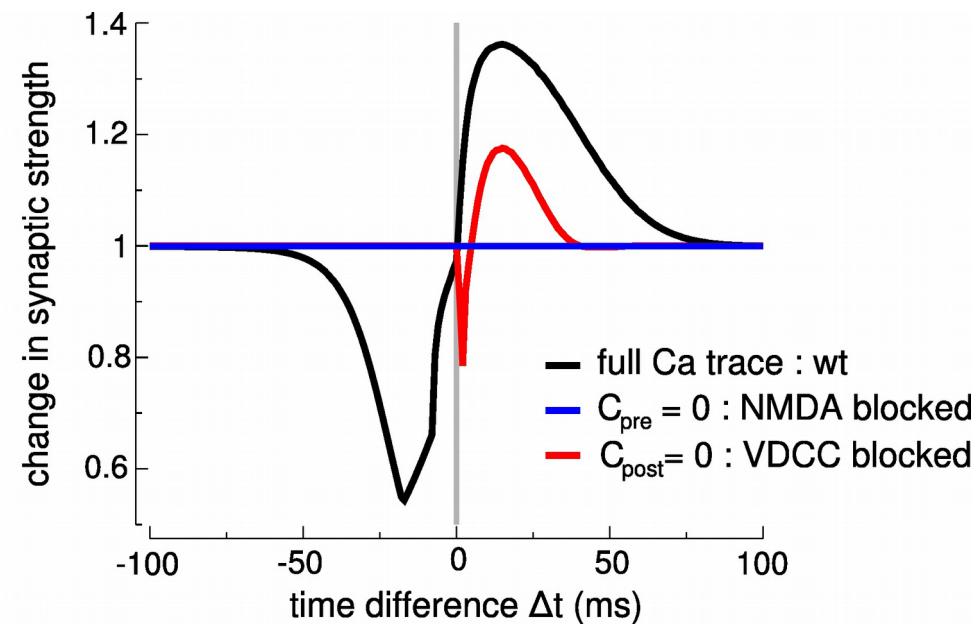
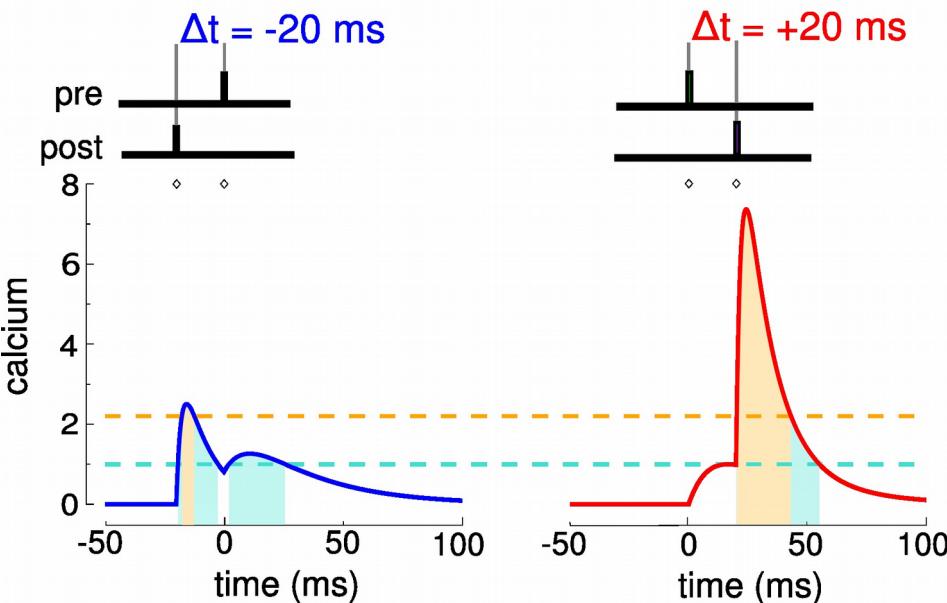
### 3.1 Diversity of plasticity outcomes

# Malleability of hippocampal STDP explained by $\text{Ca}^{2+}$



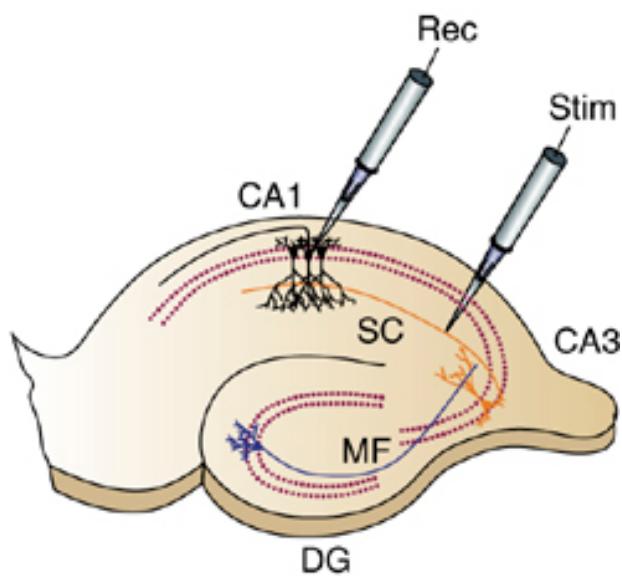
[Wittenberg & Wang, 2006]

# Pharmacological manipulations explained by $\text{Ca}^{2+}$

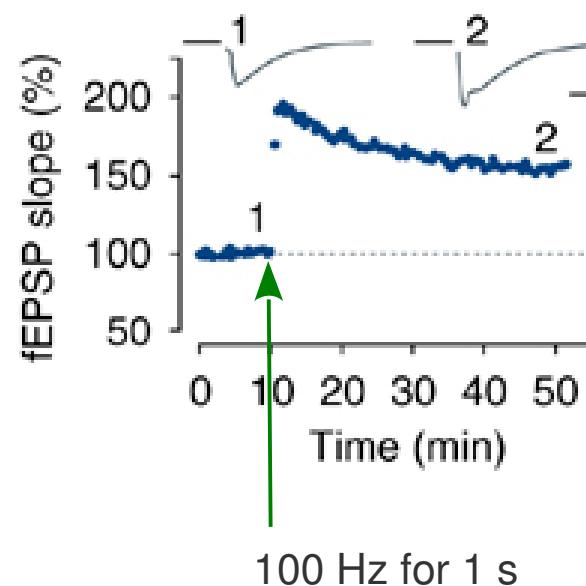


[Bi & Poo, 1998; Nevian & Sakmann, 2006]

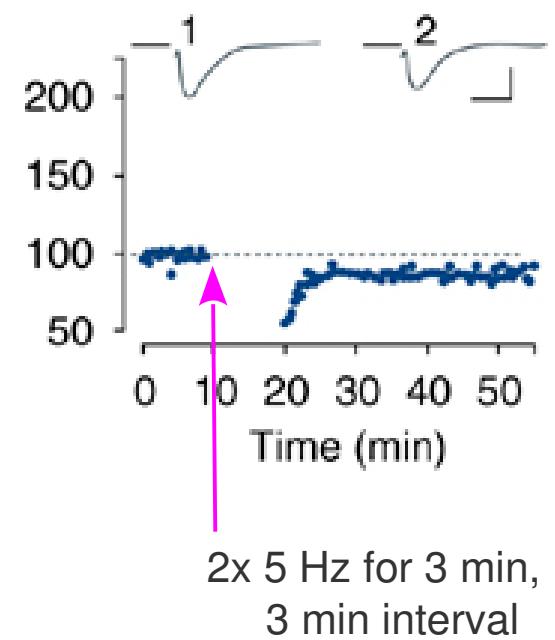
- nonlinear, finite rise time calcium transients necessary to reproduce pharmacological block experiments



long-term potentiation  
LTP

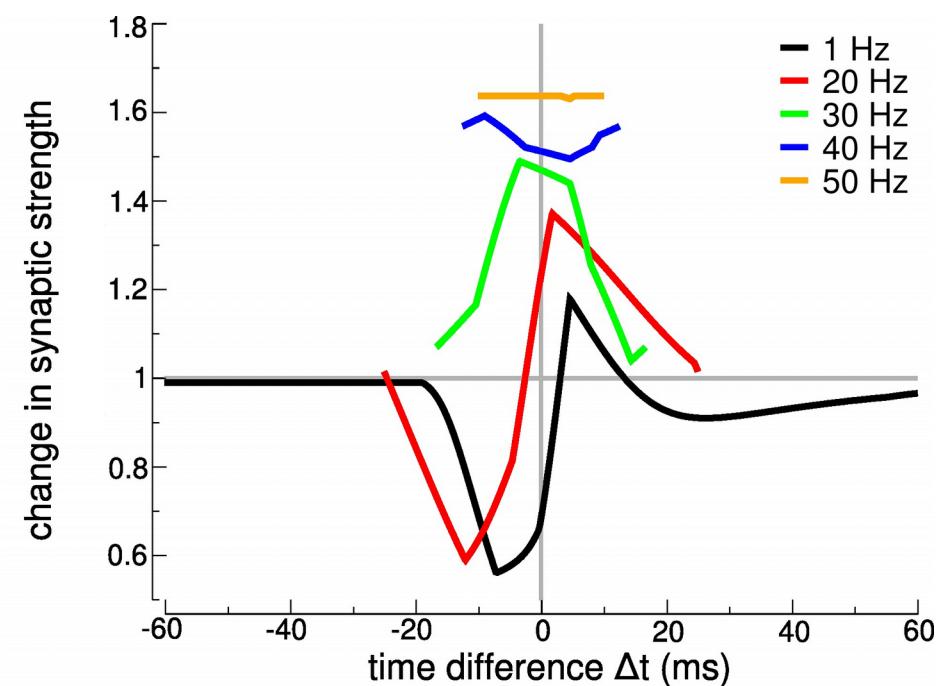
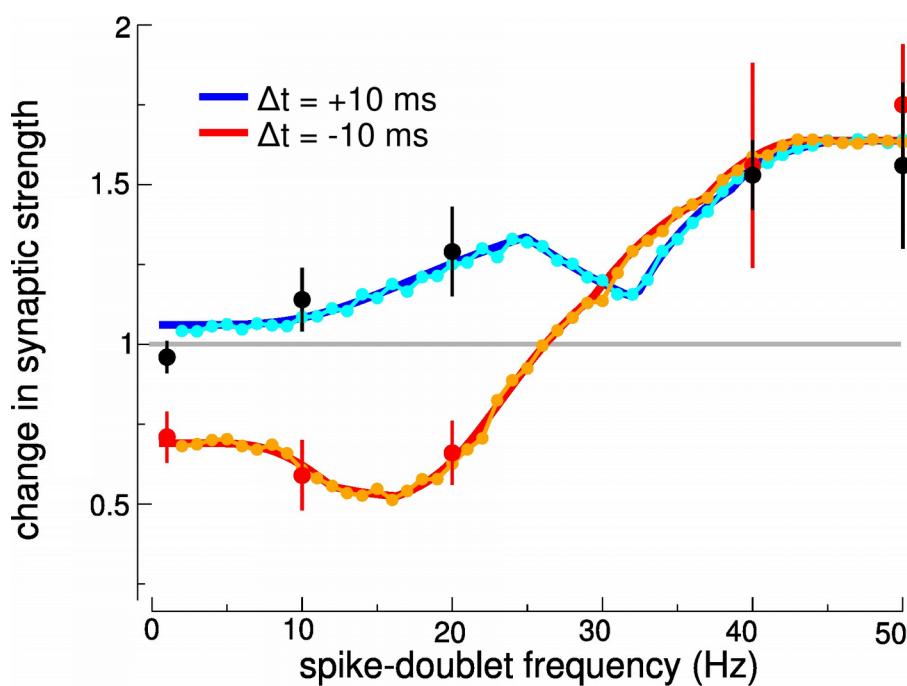
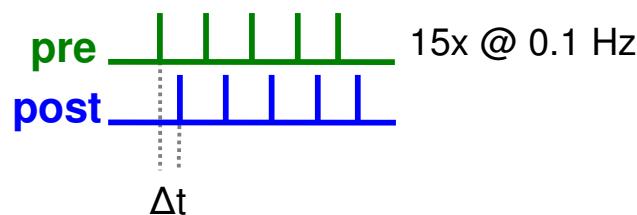


long-term depression  
LTD



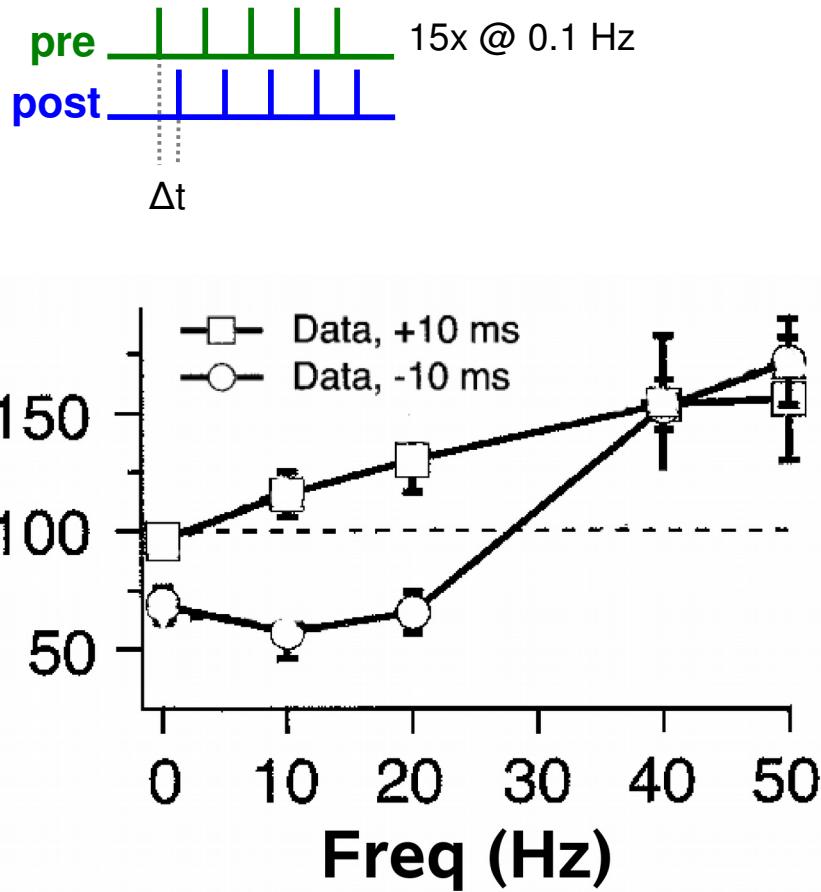
[Morishita *et al.*, 2005]

# Firing rate dependence in cortical slices



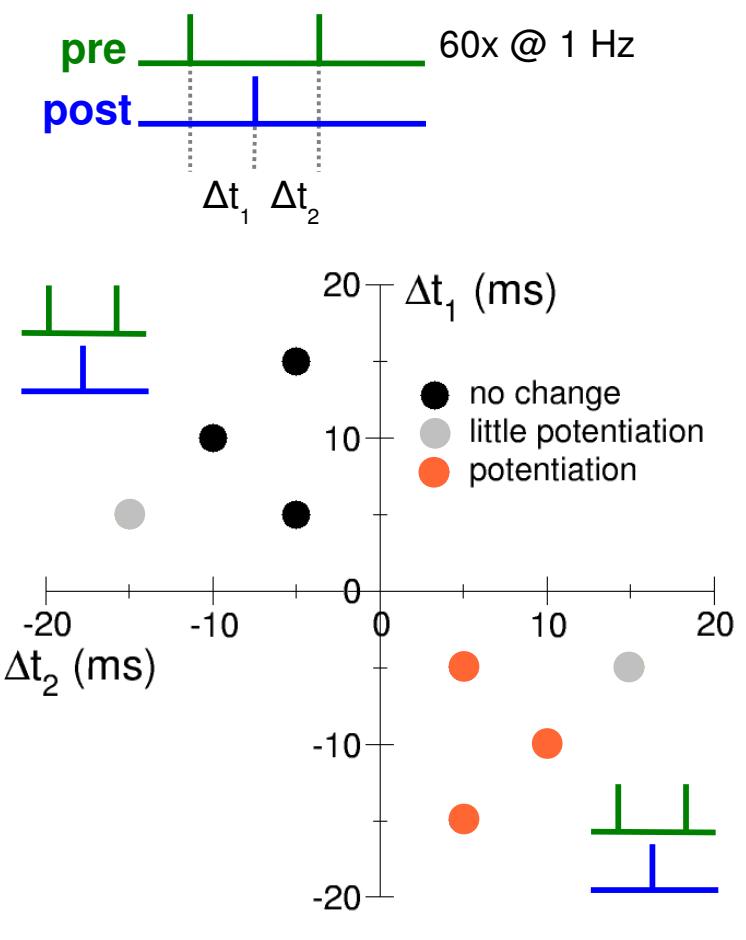
[Sjöström *et al.*, 2001]

## spike-pair & frequency



[Sjöström *et al.*, 2001]

## spike - triplets



[Wang *et al.*, 2005]